

# edgeR: differential expression analysis of digital gene expression data

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## 1 Introduction

This document gives a brief introduction and overview of the R Bioconductor package **edgeR** [Robinson and Smyth, 2007, 2008], which provides statistical routines for determining differential expression in digital gene expression data. The routines can be applied equally to SAGE, CAGE, Illumina/Solexa, 454 or ABI SOLiD experiments. In fact, the methods may be useful in other experiments where counts are observed.

The package can easily be loaded into an R session:

```
> library(edgeR)
```

R packages for the processing of raw data files for digital gene expression (DGE) datasets are still in development stages (e.g. **ShortRead**) at time of writing. The methods presented here require a **DGEList** object as a starting point.

## 2 Reading data

We assume that the data are stored in one of two formats. Either there is a single file containing a table of counts with the first column containing the tag identifiers and the remaining columns containing the tag counts for each library sequenced, or there is an individual file for each library, each with first column for tag identifiers and second column for counts.

If the counts for all libraries are stored in a single file, then an appropriate in-built R function (such as **read.delim** or **read.csv**) can be used to read the table of counts into R. The library sizes can be the column sums from the table of counts, and thus easily obtained, or the user can specify the the library sizes through **lib.size** argument of the **DGEList()** constructor. See the help documentation (**?DGEList** or **"DGEList-class"**) or the examples below for further details.

If the counts are stored in separate files, then, given a vector containing the filenames the **edgeR** function **readDGE** will read in the data from the individual files, collate the counts into a table and

compute the library sizes and return a `DGEList` object. See the help documentation (`?readDGE`) or the examples below for further details.

### 3 Moderated negative binomial dispersions

The basic model we use for DGE data is based on the negative binomial distribution. The model is very flexible. For example, if  $Y$  is distributed as  $NB(\mu, \phi)$ , then the expected value of  $Y$  is  $\mu$  and the variance is  $\mu + \mu^2 \cdot \phi$ , thus giving sufficient flexibility for many scenarios in observing count data.

The observed data can be denoted as  $Y_{gij}$  where  $g$  is the gene (tag, exon, etc.),  $i$  is the experimental group and  $j$  is the index of the replicate. We can model the counts as

$$Y_{gij} \sim NB(M_j \cdot p_{gi}, \phi_g)$$

where  $p_{gi}$  represents the proportion of the sequenced sample for group  $i$  that is tag  $g$  and  $M_j$  represents the library size.

It is of interest to find genes where, for example,  $p_{g1}$  is significantly different from  $p_{g2}$ . The parameter  $\phi_g$  is the overdispersion (relative to the Poisson) and represents the biological, or sample-to-sample variability. The methods we developed moderate the dispersion estimates towards a common dispersion, much like how the `limma` package moderates the variances in the analysis of microarray data. It is also possible to analyse DGE data using a common dispersion for each tag using `edgeR`.

## 4 Case study: SAGE data

### 4.1 Introduction

This section provides a detailed analysis of data from a SAGE experiment to illustrate the data analysis pipeline for `edgeR`. The data come from a very early study using SAGE technology to analyse gene expression profiles in human cancer cells [Zhang et al., 1997].

### 4.2 Source of the data

At the time that Zhang et al. [1997] published their paper, no comprehensive study of gene expression in cancer cells had been reported. Zhang et al. [1997] designed a study to address the following issues:

1. How many genes are expressed differentially in tumour versus normal cells?
2. Are the majority of those differences cell-autonomous rather than dependent on the tumour micro-environment?
3. Are most differences cell type-specific or tumour-specific?

They used normal and neoplastic gastro-intestinal tissue as a prototype and analysed global profiles of gene expression in human cancer cells. The researchers derived transcripts from human colorectal (CR) epithelium, CR cancers or pancreatic cancers. The data that we analyse in this case study are Zhang et al. [1997]’s SAGE results for the comparison of expression patterns between normal colon epithelium and primary colon cancer.

They report that the expression profiles revealed that most transcripts were expressed at similar levels, but that 289 transcripts were expressed at significantly different levels [ $P$ -value  $< 0.01$ ] and that 181 of these 289 were decreased in colon tumours as compared with normal colon tissue. Zhang et al. [1997] used Monte Carlo simulation to determine statistical significance. In this case study we will use the **edgeR** package, based around the negative binomial model, to identify genes differentially expressed in the normal and cancer samples.

### 4.3 Reading in the data and creating a **DGEList** object

Our first task is to load the **edgeR** package, read the data into R and organise the data into a **DGEList** object that the functions in the package can recognise. The library size is usually the total sum of all of the counts for a library, and that is how library size is defined in this analysis. The easiest way to construct an appropriate **DGEList** object for these data is described below.

In this case, the tag counts for the four individual libraries are stored in four separate plain text files, **GSM728.txt**, **GSM729.txt**, **GSM755.txt** and **GSM756.txt**. In each file, the tag IDs and counts for each tag are provided in a table. It is best to create a tab-delimited, plain-text ‘Targets’ file, which, under the headings ‘files’, ‘group’ and ‘description’, gives the filename, the group and a brief description for each sample.

The **targets** object is produced when the ‘Targets.txt’ file is read into the R session. This object makes a convenient argument to the function **readDGE** which reads the tables of counts into our R session, calculates the sizes of the count libraries and produces a **DGEList** object for use by subsequent functions.

```
> library(edgeR)
> setwd("/Users/davismcc/Documents/Honours/Data/ZhangData")
> targets <- read.delim(file = "Targets.txt", stringsAsFactors = FALSE)
> targets
```

	files	group	description
1	GSM728.txt	NC	Normal colon
2	GSM729.txt	NC	Normal colon
3	GSM755.txt	Tu	Primary colonrectal tumour
4	GSM756.txt	Tu	Primary colonrectal tumour

```
> d <- readDGE(targets, skip = 5, comment.char = "#")
> d
```

An object of class "DGEList"

\$samples

	files	group	description	lib.size
GSM728	GSM728.txt	NC	Normal colon	50179
GSM729	GSM729.txt	NC	Normal colon	49593
GSM755	GSM755.txt	Tu Primary	colonrectal tumour	57686
GSM756	GSM756.txt	Tu Primary	colonrectal tumour	49064

\$counts

	GSM728	GSM729	GSM755	GSM756
CCCATCGTCC	1288	1380	1236	0
CCTCCAGCTA	719	458	148	142
CTAAGACTTC	559	558	248	199
GCCCAGGTCA	520	448	22	62
CACCTAATTG	469	472	763	421

57443 more rows ...

This `DGEList` is now ready to be passed to the functions that do the calculations to determine differential expression levels for the genes. Note that when we ‘see’ the `DGEList` object `d`, the counts for just the first five genes in the table are shown, as well as the library sizes and groups for the samples.

## 4.4 Analysis using common dispersion

### 4.4.1 Estimating the common dispersion

The first major step in the analysis of DGE data using the NB model is to estimate the dispersion parameter for each tag. The most straight-forward analysis of DGE data uses the common dispersion estimate as the dispersion for all tags. For many applications this will be adequate and it may not be necessary to estimate tagwise dispersions, i.e. estimate the dispersion parameter separately for each tag. Using the common dispersion allows the user to obtain DE results very quickly and in few steps, and so makes a good place to start with any analysis of DGE data.

Estimating the common dispersion is done using the function `estimateCommonDisp`. In order to do this, the function first needs to generate the ‘pseudocounts’ under the alternative hypothesis (that there really is a difference in expression level between the groups). The conditional maximum likelihood method assumes that the library sizes are equal, which is certainly not true in general for DGE data.

The pseudocounts are calculated using a quantile-to-quantile method for the negative binomial distribution so that the library sizes for the pseudocounts are equal to the geometric mean of the original library sizes. These pseudocounts are then used as the count data for the common conditional negative binomial likelihood function, which is maximised over the dispersion parameter to obtain our estimate of the common dispersion.

```

> d <- estimateCommonDisp(d)
> names(d)

[1] "samples"          "common.dispersion" "counts"
[4] "pseudo.alt"       "conc"              "common.lib.size"

```

The output of `estimateCommonDisp` is a `DGEList` object with several new elements. The element `common.dispersion`, as the name suggests, provides the estimate of the common dispersion, and `pseudo.alt` gives the pseudocounts calculated under the alternative hypothesis. The element `conc` gives the estimates of the overall concentration of each tag across all of the original samples (`conc$conc.common`) and the estimate of the concentration of each tag within each group (`conc$conc.group`). The element `common.lib.size` gives the library size to which the original libraries have been adjusted in the pseudocounts.

We see in the output below that the total number of counts in each library of the pseudocounts agrees well with the common library size, as desired.

```

> d$samples$lib.size

[1] 50179 49593 57686 49064

> d$common.lib.size

[1] 51516

> colSums(d$pseudo.alt)

GSM728 GSM729 GSM755 GSM756
51512  51513  51674  51483

```

Under the negative binomial model, the square root of the common dispersion gives the coefficient of variation of biological variation. Here, as seen in the code below, the coefficient of variation of biological variation is found to be 0.45. We also note that a common dispersion estimate of 0.2 means that there is a lot more variability in the data that can be accounted for by the Poisson model—if a tag has just 200 counts, then the estimate of the tag’s variance under the NB model is over 40 times greater than it would be under the Poisson model.

```

> d$common.dispersion

[1] 0.1988

> sqrt(d$common.dispersion)

[1] 0.4458

```

#### 4.4.2 Testing

Once we have an estimate of the common dispersion, we can proceed with testing procedures for determining differential expression. The **edgeR** package uses an exact test for the negative binomial distribution, which has strong parallels with Fisher's exact test, to compute exact  $p$ -values that can be used to assess differential expression. The function **exactTest** allows the user to conduct the NB exact test for pairwise comparisons of groups. Here there are only two groups, so the pair need not be specified—the function by default compares the two groups present.

```
> de.com <- exactTest(d)

Comparison of groups: Tu - NC

> names(de.com)

[1] "table"      "comparison"

> names(de.com$table)

[1] "logConc" "logFC"    "p.value"
```

The object produced by **exactTest** contains two elements: **table** and **comparison**. The element **de.com\$comparison** contains a vector giving the names of the two groups compared. The **de.com\$table** contains the elements **logConc**, which gives the overall concentration for a tag across the two groups being compared, **logFC**, which gives the log-fold change difference for the counts between the groups and **p.value** gives the exact  $p$ -values computed.

The results of the NB exact test can be accessed conveniently using the **topTags** function applied to the object produced by **exactTest**. The user can specify the number, **n**, of tags for which they would like to see the differential expression information, ranked by  $p$ -value (default) or fold change. As the same test is conducted for many thousands of tags, adjusting the  $p$ -values for multiple testing is recommended. The desired adjustment method can be supplied by the user, with the default method being Benjamini and Hochberg's approach for controlling the false discovery rate (FDR) [Benjamini and Hochberg, 1995]. The table below shows the top 10 DE genes ranked by  $p$ -value.

The output below shows that the **edgeR** package identifies a good deal of differential expression between the normal colon cell group and the primary CR cancer cell group. The top DE genes are given very small  $p$ -values, even after adjusting for multiple testing. Furthermore, all of the top genes have a large fold change, indicating that these genes are more likely to be biologically meaningful. A Gene Ontology analysis could be carried out using the list of top genes and  $p$ -values provided by **topTags** in order to obtain more systematic and functional information about the differentially expressed genes.

```
> options(digits = 4)
> topTags(de.com)
```

```

Comparison of groups: Tu - NC
      logConc  logFC   PValue    FDR
AGCTGTTCCC  -28.24  43.552 1.017e-19 5.841e-15
CTTGGGTTTT  -29.88  40.271 2.967e-10 8.522e-06
TACAAAATCG  -30.26  39.510 2.712e-08 4.926e-04
CCCAACGCGC  -12.80  -5.849 3.430e-08 4.926e-04
GCCACCCCT   -30.33  39.380 6.341e-08 7.285e-04
CCAGTCCGCC  -30.43  39.177 1.844e-07 1.513e-03
GTCATCACCA  -30.42 -39.189 1.844e-07 1.513e-03
TCACCGGTCA  -11.13  -4.229 4.428e-07 3.180e-03
TAAATTGCAA  -11.39  -4.242 6.090e-07 3.887e-03
CGCGTACTA   -12.30   4.611 7.300e-07 4.194e-03

```

The table below shows the raw counts for the genes that `edgeR` has identified as the most differentially expressed. For these genes there seems to be very large differences between the groups, suggesting that the DE genes identified are truly differentially expressed, and not false positives.

```

> detags.com <- rownames(topTags(de.com)$table)
> d$counts[detags.com, ]

```

	GSM728	GSM729	GSM755	GSM756
AGCTGTTCCC	0	0	119	1011
CTTGGGTTTT	0	0	21	97
TACAAAATCG	0	0	14	56
CCCAACGCGC	106	1	2	0
GCCACCCCT	0	0	5	58
CCAGTCCGCC	0	0	6	49
GTCATCACCA	35	20	0	0
TCACCGGTCA	118	75	6	5
TAAATTGCAA	103	59	3	6
CGCGTACTA	1	3	88	21

If we order the genes by fold change instead of  $p$ -value, as in the table below, we see that the genes with the largest fold changes have very small concentrations. This ranking is dominated by genes that have zero total counts in one group and is less informative than ranking by  $p$ -value.

```

> topTags(de.com, sort.by = "logFC")

```

```

Comparison of groups: Tu - NC
      logConc  logFC   PValue    FDR
AGCTGTTCCC  -28.24  43.55 1.017e-19 5.841e-15
CTTGGGTTTT  -29.88  40.27 2.967e-10 8.522e-06

```

TACAAAATCG	-30.26	39.51	2.712e-08	4.926e-04
GCCACCCCCT	-30.33	39.38	6.341e-08	7.285e-04
GTCATCACCA	-30.42	-39.19	1.844e-07	1.513e-03
CCAGTCCGCC	-30.43	39.18	1.844e-07	1.513e-03
GTGCGCTGAG	-30.67	38.69	2.362e-06	9.048e-03
CTTGACATAC	-30.69	-38.66	2.837e-06	9.588e-03
GTGTGTTTGT	-30.72	38.59	4.135e-06	1.320e-02
GGGGGGGGGG	-30.74	38.56	5.019e-06	1.518e-02

Zhang et al. [1997] identified 289 genes as significantly differentially expressed with  $p$ -values less than 0.01. We can look at the genes that are given an exact  $p$ -value less than 0.01 by **edgeR** before adjusting for multiple testing, and less than 0.05 after adjustment.

We see in the output below that 264 genes are significantly differentially expressed according to **edgeR** when using the common dispersion estimate. Of those genes, 100 are up-regulated in the cancer cells compared with the normal cells and 164 are down-regulated in the cancer cells compared with normal cells. These proportions of up- and down-regulated tags are very similar to those found by Zhang et al. [1997].

```
> sum(de.com$table$p.value < 0.01)
```

```
[1] 264
```

```
> top264 <- topTags(de.com, n = 264)
> sum(top264$table$logFC > 0)
```

```
[1] 100
```

```
> sum(top264$table$logFC < 0)
```

```
[1] 164
```

Furthermore, we see below that 33 tags (0.06% of the total number) have a  $p$ -value of less than 0.05 after adjusting for multiple testing using the Benjamini and Hochberg [1995] method for controlling the FDR, which is strong evidence for differential expression.

```
> sum(p.adjust(de.com$table$p.value, method = "BH") < 0.05)
```

```
[1] 33
```

```
> mean(p.adjust(de.com$table$p.value, method = "BH") < 0.05) *
+      100
```

```
[1] 0.05744
```



### 4.4.3 Visualising DGE results

The function `plotSmear` can be used to generate a plot of the log-fold change against the log-concentration for each tag (analogous to an MA-plot in the microarray context). We can easily identify the top DE tags and highlight them on the plot. The code for producing the default fold-change plot is shown below, and the result of this code is shown in Figure 5.

```
> detags264 <- rownames(topTags(de.com, n = 264)$table)
> plotSmear(d, de.tags = detags264, main = "FC plot using common dispersion")
> abline(h = c(-2, 2), col = "dodgerblue")
```

Figure 5 shows the default fold change-plot for these data—the ‘smear plot’. Plotting DGE data poses some challenges, as when the total counts in one group are zero, the log-fold change is technically infinite, and the log-concentration is negative infinity. With the algorithm used by `topTags`, we see very high log-fold changes and very small values for log-concentration for such tags, but plotting these values directly causes problems with the scale of the graph. To get around this problem, `edgeR` produces a ‘smear’ of points at the left-most edge of the plot for tags which have zero counts in one of the groups. Although this is still slightly artificial, it has the advantage that the expression level of all tags can be visualised and interpreted simultaneously.

The ‘lines’ of points we see at smaller log-concentration values arise from the discrete nature of the count data. When the sum all of the counts in one of the groups is one, we see the lines of points furthest away from the main body of points, and other lines of points correspond to when the total sum of counts in one of the groups is 2, 3, 4 and so on.

In Figure 5, the 264 tags identified as differentially expressed (i.e. those identified as significant ( $p$ -value less than 0.01) by `edgeR` using the common dispersion) are outlined in red.

## 4.5 Analysing the data using moderated tagwise dispersions

### 4.5.1 Estimating the tagwise dispersion

An extension to simply using the common dispersion for each tag is to estimate the dispersion separately for each tag, while ‘squeezing’ these estimates towards the common dispersion estimate in order to improve inference by sharing information between tags. This type of analysis can also be carried out in few steps using the `edgeR` package.

As noted earlier, the dispersion parameter is the overdispersion relative to the Poisson, and represents the biological, or sample-to-sample variability. The methods we developed moderate the dispersion estimates towards a common dispersion, much like how the `limma` package moderates the variances in the analysis of microarray data.

To run the moderated analysis, we need to determine how much moderation is necessary. For this, we can use an empirical Bayes rule that involves calculating a weight parameter `prior.n`. However, for many applications (especially if the estimated smoothing parameter is large), using the common dispersion for all tags will give excellent results.

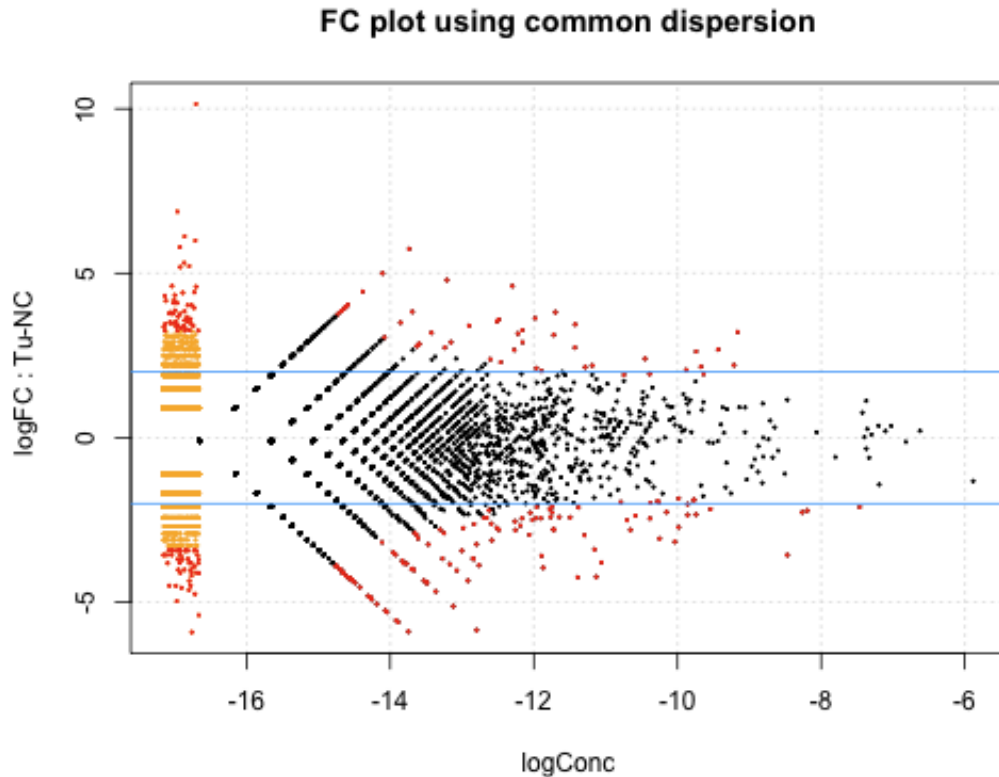


Figure 1: Plot of the log-fold change against the log-concentration for each tag. The 264 most differentially expressed tags as identified by `edgeR` using the common dispersion are outlined in red.

In order to determine how much moderation is necessary, we require an estimate of the dispersion parameter, so we use the common dispersion estimate from `estimateCommonDisp`. The smoothing parameter, `prior.n` can then be calculated. As we see below, for this dataset the estimate of the smoothing parameter is very large, so if we were to use this large value for the weight parameter we would moderate the tagwise dispersion estimates so strongly that it would be equivalent to using the common dispersion estimate.

```
> prior.n <- estimateSmoothing(d)
> prior.n
```

```
[1] 29481
```

Alternatively, the value for the weight parameter `prior.n` can be selected *a priori*, instead of being estimated. In an experiment such as that we consider here, in which we have just four

samples, two in each group, and thus two degrees of freedom for estimating the dispersion parameter, setting the `prior.n` to be relatively large should be appropriate, so that individual tagwise dispersion estimates are ‘squeezed’ quite strongly towards the common dispersion. Here, we choose `prior.n` to be 100. This means that the common likelihood receives the weight of 100 individual tags, so there will be a reasonable degree of ‘squeezing’, but there is still scope to estimate an individual dispersion for each gene.

The function `estimateTagwiseDisp` produces a `DGEList` object that contains all of the elements present in the object produced by `estimateCommonDisp`, as well as the value for `prior.n` used (`d$prior.n`) and the tagwise dispersion estimates (`d$tagwise.dispersion`), as we see below.

```
> d <- estimateTagwiseDisp(d, prior.n = 100)
```

Using grid search to estimate tagwise dispersion.

```
> names(d)
```

```
[1] "samples"           "common.dispersion" "prior.n"
[4] "tagwise.dispersion" "counts"           "pseudo.alt"
[7] "conc"              "common.lib.size"
```

```
> d$prior.n
```

```
[1] 100
```

```
> head(d$tagwise.dispersion)
```

```
[1] 0.99002 0.12528 0.08252 0.22934 0.11896 0.15795
```

It is interesting to consider the distribution of the tagwise dispersion estimates. As we can see from the output below, the tagwise dispersion estimates range from a minimum of 0.08 to a maximum of 0.99, but the tags in the middle two quartiles of the tagwise dispersion estimates have dispersion estimates just slightly larger than the common dispersion estimate.

```
> summary(d$tagwise.dispersion)
```

```
   Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
0.0825  0.2000  0.2000  0.2000  0.2000  0.9900
```

```
> d$common.dispersion
```

```
[1] 0.1988
```

### 4.5.2 Testing

The testing procedures when using tagwise dispersion estimates are carried out exactly as for the common dispersion, as described above, but we add the argument `common.disp=FALSE` to the call to `exactTest`.

```
> de.tgw <- exactTest(d, common.disp = FALSE)
```

Comparison of groups: Tu - NC

The output below shows that when using tagwise dispersions, the `edgeR` package still identifies a lot of differential expression between the normal colon cell group and the primary CR cancer cell group. The top DE tags are given very small  $p$ -values, even after adjusting for multiple testing. As with the analysis using the common dispersion, all of the top tags have a large fold change, indicating that these changes in expression are likely to be biologically meaningful. We note that the ranking is different, however, and not all of the top ten tags according to using the common dispersion are found to be among the top ten tags using tagwise dispersions.

```
> topTags(de.tgw)
```

Comparison of groups: Tu - NC

	logConc	logFC	PValue	FDR
AGCTGTTCCC	-28.240	43.553	1.541e-10	8.855e-06
TCACCGGTCA	-11.130	-4.229	3.892e-09	1.118e-04
GTCATCACCA	-30.421	-39.189	7.815e-08	1.497e-03
TAAATTGCAA	-11.390	-4.244	1.846e-07	2.355e-03
CTTGGGTTTT	-29.879	40.274	2.049e-07	2.355e-03
TAATTTTTGC	-13.735	5.741	4.550e-07	4.356e-03
CTTGACATAC	-30.687	-38.658	5.735e-07	4.378e-03
ATTTCAAGAT	-13.747	-5.893	6.097e-07	4.378e-03
TGCTCCTACC	-9.985	-2.722	7.139e-07	4.407e-03
GTGCGCTGAG	-30.672	38.688	7.671e-07	4.407e-03

The table below shows the raw counts for the tags that `edgeR` has identified as the most differentially expressed using tagwise dispersions. For these genes there seems to be very large differences between the groups, suggesting that the DE genes identified are truly differentially expressed, and not false positives.

We note that in general, when using tagwise dispersions, the counts are more consistent within groups, as using tagwise dispersions instead of the common dispersion penalises tags which are highly variable within groups. The smaller the value selected for `prior.n`, the more highly variable tags will be penalised, as there is less ‘squeezing’ of the tagwise dispersions towards the common value.

```
> detags.tgw <- rownames(topTags(de.tgw)$table)
> d$counts[detags.tgw, ]
```

	GSM728	GSM729	GSM755	GSM756
AGCTGTTCCC	0	0	119	1011
TCACCGGTCA	118	75	6	5
GTCATCACCA	35	20	0	0
TAAATTGCAA	103	59	3	6
CTTGGGTTTT	0	0	21	97
TAATTTTTGC	0	1	37	21
CTTGACATAC	18	20	0	0
ATTTCAAGAT	35	21	0	1
TGCTCCTACC	140	113	22	19
GTGCGCTGAG	0	0	18	23

Of course, we can sort the top table differently, as we did earlier.

We see in the output below that 254 genes are significantly differentially expressed according to `edgeR` when using the tagwise dispersion estimates (ten fewer than when using the common dispersion). Of those tags, 87 are up-regulated in the cancer cells compared with the normal cells and 167 are down-regulated in the cancer cells compared with normal cells. These proportions of up- and down-regulated tags are similar to those found using the common dispersion, but there is a slightly higher proportion of down-regulated tags in those identified as DE using tagwise dispersions.

```
> sum(de.tgw$table$p.value < 0.01)
```

```
[1] 254
```

```
> top254 <- topTags(de.tgw, n = 254)
```

```
> sum(top254$table$logFC > 0)
```

```
[1] 87
```

```
> sum(top254$table$logFC < 0)
```

```
[1] 167
```

Furthermore, we see below that 28 tags (0.05% of the total number) have a  $p$ -value of less than 0.05 after adjusting for multiple testing using the Benjamini and Hochberg [1995] method for controlling the FDR, which is strong evidence for differential expression.

```
> sum(p.adjust(de.tgw$table$p.value, method = "BH") < 0.05)
```

```
[1] 28
```

```
> mean(p.adjust(de.tgw$table$p.value, method = "BH") < 0.05) *  
+      100
```

```
[1] 0.04874
```

### 4.5.3 Visualising DGE results

Shown below is the code for producing the default fold-change plot using `plotSmear` with the DE tags as determined using tagwise dispersions highlighted, and the result of this code is shown in Figure 6.

```
> detags254 <- rownames(topTags(de.tgw, n = 254)$table)

> plotSmear(d, de.tags = detags254, main = "FC plot using tagwise dispersions")
> abline(h = c(-2, 2), col = "dodgerblue")
```

In Figure 6, the 254 tags identified as differentially expressed (i.e. those identified as significant ( $p$ -value less than 0.01) by `edgeR` using the tagwise dispersions) are highlighted in red. We see that the pattern of differential expression using tagwise dispersions that we see in Figure 6 is very similar to that obtained using the common dispersion that we saw in Figure 5.

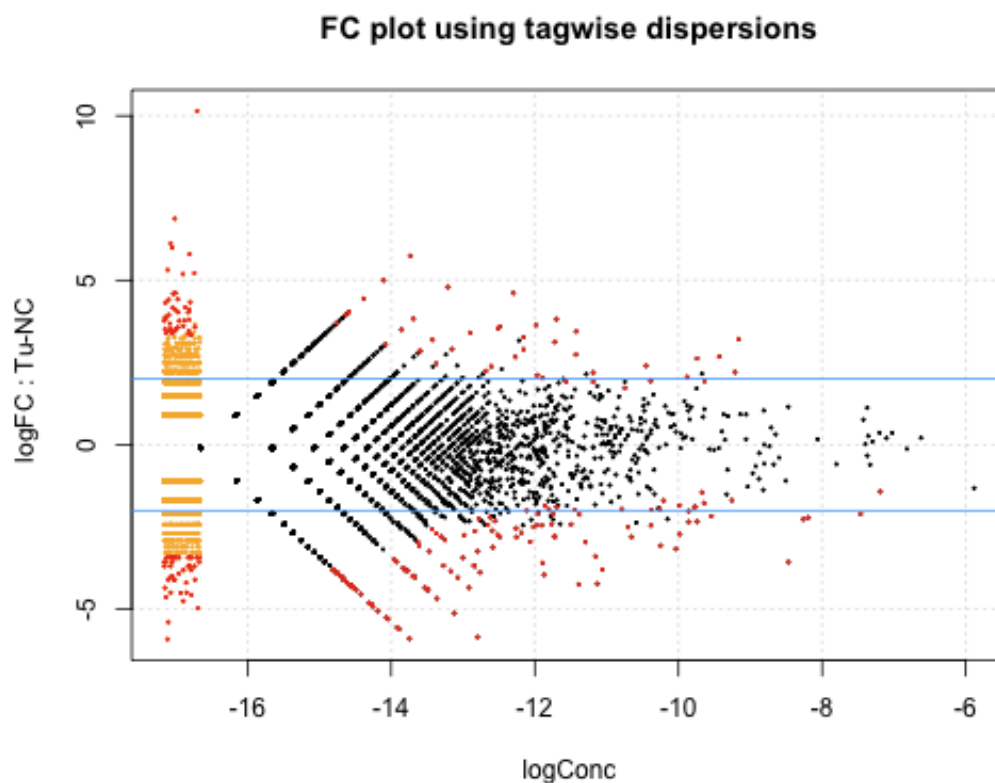


Figure 2: Plot of the log-fold change against the log-concentration for each tag. The 264 most differentially expressed tags as identified by `edgeR` are outlined in red.

## 4.6 Setup

This analysis of Zhang et al. [1997]’s SAGE data was conducted on:

```
> sessionInfo()
```

```
R version 2.9.1 (2009-06-26)
```

```
i386-apple-darwin8.11.1
```

```
locale:
```

```
en_AU.UTF-8/en_AU.UTF-8/C/C/en_AU.UTF-8/en_AU.UTF-8
```

```
attached base packages:
```

```
[1] stats      graphics  grDevices  utils      datasets  methods   base
```

```
other attached packages:
```

```
[1] edgeR_1.3.6
```

```
loaded via a namespace (and not attached):
```

```
[1] limma_2.18.2
```

and took 2–3 minutes to carry out on an Apple MacBook with a 2.4 Ghz Intel Core 2 Duo processor and 4 Gb of 1067 MHz DDR3 memory.

## 5 Case Study: deep-sequenced short tags

### 5.1 Introduction

This section provides a detailed analysis of data from an experiment seeking to compare deep-sequenced tag-based expression profiling to the microarray platforms that had been previously used to conduct such studies [’t Hoen et al., 2008].

### 5.2 Source of the data

’t Hoen et al. [2008] address both biological and technical questions in their study. The biological question addressed was the identification of transcripts differentially expressed in the hippocampus between wild-type mice and transgenic mice overexpressing a splice variant of the  $\delta$ C-doublecortin-like kinase-1 (*Dclk1*) gene. The splice variant, DCLK-short, makes the kinase constitutively active and causes subtle behavioural phenotypes.

On the technical side, the researchers compare the robustness, resolution and inter-lab portability of Solexa/Illumina’s DGE tag profiling approach and five microarray platforms [’t Hoen et al., 2008]. The tag-based gene expression technology in this experiment could be thought of as a hybrid between SAGE and RNA-seq—like SAGE it uses short sequence tags ( $\sim 17$ bp) to identify

transcripts, but it uses the deep sequencing capabilities of Solexa/Illumina 1G Genome Analyzer to greatly increase the number of tags that can be sequenced. For our purposes we will concentrate solely on the DGE data generated in the experiment.

The RNA samples came from wild-type male C57/BL6j mice and transgenic mice overexpressing DCLK-short with a C57/BL6j background. Tissue samples were collected from four individuals in each of the two groups by dissecting out both hippocampi from each mouse. Total RNA was isolated and extracted from the hippocampus cells and sequence tags were prepared using Illumina's Digital Gene Expression Tag Profiling Kit according to the manufacturer's protocol.

Sequencing was done using Solexa/Illumina's Whole Genome Sequencer. RNA from each biological sample was supplied to an individual lane in one Illumina 1G flowcell. The instrument conducted 18 cycles of base incorporation, then image analysis and basecalling were performed using the Illumina Pipeline. Sorting and counting the unique tags followed, and the raw data (tag sequences and counts) are what we will analyze here. 't Hoen et al. [2008] went on to annotate the tags by mapping them back to the genome. In general, the mapping of tags is an important and highly non-trivial part of a DGE experiment, but we shall not deal with this task in this case study.

The researchers obtained  $\sim 2.4$  million sequence tags per sample, with tag abundance spanning four orders of magnitude. They found the results to be highly reproducible, even across laboratories. Using a dedicated Bayesian model, they found 3179 transcripts to be differentially expressed with a FDR of 8.5%. This is a much higher figure than was found for the microarrays. 't Hoen et al. [2008] conclude that deep-sequencing offers a major advance in robustness, comparability and richness of expression profiling data.

### 5.3 Reading in the data and creating a DGEList object

Our first task is to load the `edgeR` package, read the data into R and organise the data into an object that the functions in the package can recognise. In this case, the tag counts for the eight individual libraries are stored in eight separate plain text files, `GSM272105.txt`, `GSM272106.txt`, `GSM272318.txt`, `GSM272319.txt`, `GSM272320.txt`, `GSM272321.txt`, `GSM272322.txt` and `GSM272323.txt`.

In each file, the tag IDs and counts for each tag are provided in a table. It is best to create a tab-delimited, plain-text 'Targets' file, which, under the headings 'files', 'group' and 'description', gives the filename, the group and a brief description for each sample.

The `targets` object is produced when the 'Targets.txt' file is read into the R session. This object makes a convenient argument to the function `readDGE` which reads the tables of counts into our R session, calculates the sizes of the count libraries and produces a `DGEList` object for use by subsequent functions.

```
> setwd("/Users/davismcc/Documents/Honours/Data/Long_SAGE_Data")
> library(edgeR)
> targets <- read.delim(file = "targets.txt", stringsAsFactors = FALSE)
> targets
```



	files	group	description
1	GSM272105.txt	DCLK transgenic (Dclk1)	mouse hippocampus
2	GSM272106.txt	WT	wild-type mouse hippocampus
3	GSM272318.txt	DCLK transgenic (Dclk1)	mouse hippocampus
4	GSM272319.txt	WT	wild-type mouse hippocampus
5	GSM272320.txt	DCLK transgenic (Dclk1)	mouse hippocampus
6	GSM272321.txt	WT	wild-type mouse hippocampus
7	GSM272322.txt	DCLK transgenic (Dclk1)	mouse hippocampus
8	GSM272323.txt	WT	wild-type mouse hippocampus

```
> d <- readDGE(targets, skip = 5, comment.char = "!")
> d
```

An object of class "DGEList"

\$samples

	files	group	description
GSM272105	GSM272105.txt	DCLK transgenic (Dclk1)	mouse hippocampus
GSM272106	GSM272106.txt	WT	wild-type mouse hippocampus
GSM272318	GSM272318.txt	DCLK transgenic (Dclk1)	mouse hippocampus
GSM272319	GSM272319.txt	WT	wild-type mouse hippocampus
GSM272320	GSM272320.txt	DCLK transgenic (Dclk1)	mouse hippocampus
GSM272321	GSM272321.txt	WT	wild-type mouse hippocampus
GSM272322	GSM272322.txt	DCLK transgenic (Dclk1)	mouse hippocampus
GSM272323	GSM272323.txt	WT	wild-type mouse hippocampus

	lib.size
GSM272105	2685418
GSM272106	3517977
GSM272318	3202246
GSM272319	3558260
GSM272320	2460753
GSM272321	294909
GSM272322	651172
GSM272323	3142280

\$counts

	GSM272105	GSM272106	GSM272318	GSM272319	GSM272320
CATCGCCAGCGGGCACC	1	0	0	0	0
AAGGTCGACTCTGAAGT	1	1	0	0	0
CCTTCCTGGCTCTATGG	1	0	0	0	0
TCTGCTGAGCGTCTGTT	1	0	0	0	0
CCCCAGAGCGAATCAGG	1	1	2	1	1
	GSM272321	GSM272322	GSM272323		
CATCGCCAGCGGGCACC	0	0	0		

AAGGTCGACTCTGAAGT	0	0	0
CCTTCCTGGCTCTATGG	0	0	0
TCTGCTGAGCGTCTGTT	0	0	0
CCCCAGAGCGAATCAGG	0	2	1

844311 more rows ...

This `DGEList` is now ready to be passed to the functions that do the calculations to determine differential expression levels for the genes. Note that when we ‘see’ the `DGEList` object `d`, the counts for just the first five genes in the table are shown, as well as the `samples` element, which is a data frame constructed from the ‘Targets.txt’ file and provides the filenames, groups, descriptions and library sizes for the samples.

However, for this dataset, there were over 800 000 unique tags sequenced, most of which have a very small number of counts in total across all libraries. Since it is not possible to achieve statistical significance with fewer than six counts in total for a tag, we filter out tags with five or fewer counts in total—this also helps to speed up the calculations we need to perform. The subsetting capability of `DGEList` objects makes such filtering very easy to carry out.

```
> d <- d[rowSums(d$counts) > 5, ]
```

Now the dataset is ready to be analysed for differential expression.

## 5.4 Analysis using common dispersion

### 5.4.1 Estimating the common dispersion

As discussed for the SAGE data, the first major step in the analysis of DGE data using the NB model is to estimate the dispersion parameter for each tag. Like in the earlier case study, we begin by estimating the common dispersion using the function `estimateCommonDisp`.

```
> d <- estimateCommonDisp(d)
> names(d)

[1] "samples"          "common.dispersion" "counts"
[4] "pseudo.alt"       "conc"              "common.lib.size"
```

We see in the output below that the total counts in each library of the pseudocounts agrees well with the common library size, as desired.

```
> d$samples$lib.size

[1] 2685418 3517977 3202246 3558260 2460753 294909 651172 3142280

> d$common.lib.size
```

```
[1] 1885653
```

```
> colSums(d$pseudo.alt)
```

```
GSM272105 GSM272106 GSM272318 GSM272319 GSM272320 GSM272321 GSM272322
  1781297   1783960   1778180   1774107   1789066   1777588   1795899
GSM272323
  1783746
```

Here the coefficient of variation of biological variation (square root of the common dispersion) is found to be 0.44. We also note that a common dispersion estimate of 0.2 means that there is a lot more variability in the data that can be accounted for by the Poisson model—if a tag has just 200 counts, then the estimate of the tag’s variance under the NB model is over 40 times greater than it would be under the Poisson model.

```
> d$common.dispersion
```

```
[1] 0.1977094
```

```
> sqrt(d$common.dispersion)
```

```
[1] 0.4446452
```

### 5.4.2 Testing

Once we have an estimate of the common dispersion, we can proceed with testing procedures for determining differential expression. As for the SAGE data, there are only two groups here, so the pair need not be specified in the call to `exactTest`.

```
> de.common <- exactTest(d)
```

Comparison of groups: WT - DCLK

The results of the NB exact test can be accessed conveniently using the `topTags` function applied to the object produced by `exactTest`. The table below shows the top 10 DE genes ranked by  $p$ -value.

The table in the output from `topTags` shows that the `edgeR` package identifies a good deal of differential expression between the wild-type and the DCLK-transgenic groups. The top DE tags are given very small  $p$ -values, even after adjusting for multiple testing. Furthermore, all of the top tags have a large fold change, indicating that these tags are likely to be biologically meaningful. As suggested in the SAGE case study, a Gene Ontology analysis could be carried out using the list of top tags and  $p$ -values provided by `topTags` in order to obtain more systematic and functional information about the differentially expressed genes.

```
> topTags(de.common)
```

Comparison of groups: WT - DCLK

	logConc	logFC	PValue	FDR
AATTTCTTCCTCTTCCT	-17.29988	11.605093	1.028275e-36	1.149704e-31
CCGTCTTCTGCTTGTCG	-10.57698	5.571165	1.076926e-23	6.020501e-19
TCTGTACGCAGTCAGGC	-18.46570	-9.731983	7.100854e-23	2.646464e-18
CCGTCTTCTGCTTGTA	-14.44395	5.448158	1.083062e-21	3.027402e-17
CCGTCTTCTGCTTGTC	-15.45499	5.496920	2.759755e-20	6.171309e-16
AAGACTCAGGACTCATC	-32.27026	35.491588	7.516087e-20	1.400610e-15
CCGTCTTCTGCTTGTA	-15.57138	4.803709	3.572708e-17	5.453064e-13
AGTGTGACGTGACCGGG	-19.06213	8.067070	3.901700e-17	5.453064e-13
AAATTCTTCCTCTTCCT	-19.14713	7.910596	2.838381e-16	3.526184e-12
TGTGTATCCCACAAGGG	-18.68579	6.864501	5.262632e-16	5.884096e-12

The table below shows the raw counts for the tags that `edgeR` has identified as the most differentially expressed. For these tags there seem to be very large differences between the groups, suggesting that the DE genes identified are truly differentially expressed, and not false positives.

```
> detags.com <- rownames(topTags(de.common)$table)
```

```
> d$counts[detags.com, ]
```

	GSM272105	GSM272106	GSM272318	GSM272319	GSM272320
AATTTCTTCCTCTTCCT	1	44	0	1	0
CCGTCTTCTGCTTGTCG	106	1485	268	420	601
TCTGTACGCAGTCAGGC	160	0	101	1	440
CCGTCTTCTGCTTGTA	12	87	21	28	31
CCGTCTTCTGCTTGTC	2	42	8	17	19
AAGACTCAGGACTCATC	0	6	0	2	0
CCGTCTTCTGCTTGTA	9	61	11	20	17
AGTGTGACGTGACCGGG	0	249	0	2	1
AAATTCTTCCTCTTCCT	1	6	0	0	0
TGTGTATCCCACAAGGG	1	1	1	0	0

	GSM272321	GSM272322	GSM272323
AATTTCTTCCTCTTCCT	76	0	3487
CCGTCTTCTGCTTGTCG	5156	5	242
TCTGTACGCAGTCAGGC	0	33	0
CCGTCTTCTGCTTGTA	352	1	14
CCGTCTTCTGCTTGTC	183	1	17
AAGACTCAGGACTCATC	4	0	461
CCGTCTTCTGCTTGTA	133	0	9
AGTGTGACGTGACCGGG	5	0	85
AAATTCTTCCTCTTCCT	2	0	288
TGTGTATCCCACAAGGG	6	0	252

If we order the tags by fold change instead of  $p$ -value, as in the table below, we see that the genes with the largest fold changes have very small concentrations, and in general the  $p$ -values are not as small as when ranked by  $p$ -value (not surprisingly). This ranking is dominated by genes that have zero total counts in one group and is less informative than ranking by  $p$ -value.

```
> topTags(de.common, sort.by = "logFC")
```

Comparison of groups: WT - DCLK

	logConc	logFC	PValue	FDR
AAGACTCAGGACTCATC	-32.27026	35.49159	7.516087e-20	1.400610e-15
CCTGATGCTACAGAAAA	-32.72599	34.58013	5.104779e-15	5.188729e-11
CATAAGTCACAGAGTCG	-32.76506	-34.50198	6.541738e-14	5.626348e-10
ACTCTGTGTATTACTCC	-32.89435	34.24342	3.132417e-14	2.918603e-10
GATTTTTGTCGTGTTGG	-32.95947	34.11317	2.185773e-13	1.745636e-09
AAAAGAAATCACAGTTG	-32.96984	-34.09243	7.296827e-12	3.399379e-08
CACATAAGACTTTGGAC	-33.09656	33.83899	2.181792e-12	1.434965e-08
AAAATGTTGTTTATGGA	-33.10525	33.82162	4.049564e-12	2.156084e-08
GAAATTCTCCATTGATT	-33.13607	33.75996	4.049564e-12	2.156084e-08
AAATTATTCTCTTCCT	-33.17108	33.68995	9.017868e-12	4.033115e-08

Using their dedicated Bayesian model, 't Hoen et al. [2008] found 3179 transcripts to be differentially expressed with a FDR of 8.5%. We can compare 't Hoen et al. [2008]'s results with the results from **edgeR** by applying the **topTags** function to help look at the tags that have a FDR of less than 0.085 after adjusting for multiple testing using Benjamini and Hochberg [1995]'s method for controlling the FDR.

We see in the output below that 1710 tags (1.5% of the total number analysed) are significantly differentially expressed according to **edgeR** using the common dispersion estimate. Of those tags, 943 (55% of the DE tags) are up-regulated in the wild-type compared with the transgenic samples and 767 (45%) are down-regulated in the wild-type compared with transgenic mice.

```
> sum(p.adjust(de.common$table$p.value, method = "BH") < 0.085)
```

```
[1] 1710
```

```
> mean(p.adjust(de.common$table$p.value, method = "BH") <
+       0.085) * 100
```

```
[1] 1.529394
```

```
> top.com <- topTags(de.common, n = 1710)
```

```
> sum(top.com$table$logFC > 0)
```

```
[1] 943
```

```
> sum(top.com$table$logFC < 0)
```

```
[1] 767
```

### 5.4.3 Visualising DGE results

The code for producing the default fold-change plot, with the top 500 most DE tags highlighted in red, is shown below, and the result of this code is shown in Figure 5. In Figure 5, we see that the 500 tags identified as most differentially expressed have large fold changes—almost all of the 500 tags in red fall outside the blue lines at  $\log FC = -2$  and  $\log FC = 2$ . This means that most of these tags show at least a 4-fold change in expression level between the samples. This plot suggests strongly that the tags identified by `edgeR` as differentially expressed are truly differentially expressed, and, given the large changes in expression level, are likely to be biologically meaningful.

```
> detags500.com <- rownames(topTags(de.common, n = 500)$table)

> plotSmear(d, de.tags = detags500.com, main = "FC plot using common dispersion")
> abline(h = c(-2, 2), col = "dodgerblue", lwd = 2)
```

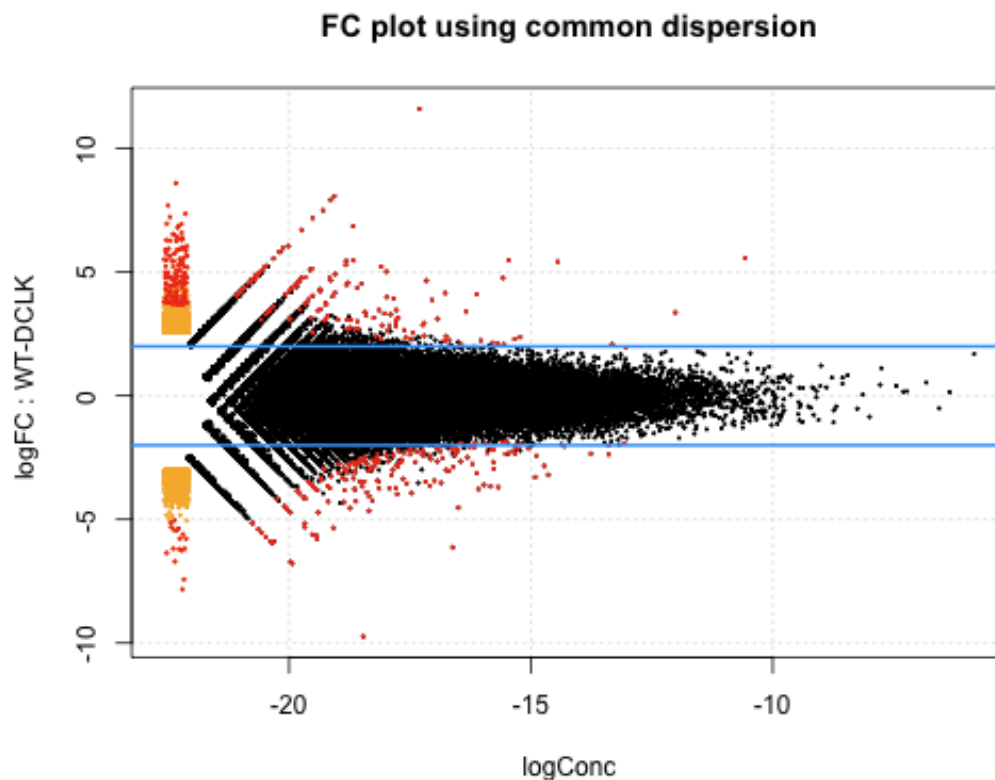


Figure 3: Plot of the log-fold change against the log-concentration for each tag. The 500 most differentially expressed tags as identified by `edgeR` using the common dispersion are outlined in red.

## 5.5 Analysis using moderated tagwise dispersions

### 5.5.1 Estimating the tagwise dispersion

An extension to simply using the common dispersion for each tag is to estimate the dispersion separately for each tag, while ‘squeezing’ these estimates towards the common dispersion estimate in order to improve inference by sharing information between tags. This type of analysis can also be carried out in few steps using the `edgeR` package.

To run the moderated analysis, we need to determine how much moderation is necessary. As discussed in the SAGE case study, we can use an empirical Bayes rule that involves calculating a weight parameter `prior.n`. However, for many applications (especially if the estimated smoothing parameter is large), using the common dispersion for all tags will give excellent results.

The smoothing parameter, `prior.n` can then be calculated using the function `estimateSmoothing`, which takes the `DGEList` object produced by `estimateCommonDisp` as its argument. As we see below, for this dataset the estimate of the smoothing parameter is very large, so if we were to use this large value for the weight parameter we would moderate the tagwise dispersion estimates so strongly that it would be equivalent to using the common dispersion estimate.

```
> prior.n <- estimateSmoothing(d)
> prior.n
```

```
[1] 15399.17
```

Alternatively, the value for the weight parameter `prior.n` can be selected *a priori*, instead of being estimated. In an experiment such as that we consider here, in which we have eight samples and thus six degrees of freedom for estimating the dispersion parameter, setting the `prior.n` to be ten should be appropriate. This means that the common likelihood receives the weight of ten individual tags, so there will be a reasonable degree of ‘squeezing’ towards the common dispersion estimate, but there is still enough scope to estimate an individual dispersion for each gene.

The function `estimateTagwiseDisp` produces a `DGEList` object that contains all of the elements present in the object produced by `estimateCommonDisp`, as well as the value for `prior.n` used (`d$prior.n`) and the tagwise dispersion estimates (`d$tagwise.dispersion`), as we see below.

```
> d <- estimateTagwiseDisp(d, prior.n = 10)
```

Using grid search to estimate tagwise dispersion.

```
> names(d)
```

```
[1] "samples"           "common.dispersion" "prior.n"
[4] "tagwise.dispersion" "counts"           "pseudo.alt"
[7] "conc"              "common.lib.size"
```

```
> d$prior.n
```

```
[1] 10
```

```
> head(d$tagwise.dispersion)
```

```
[1] 0.1997564 0.1854905 0.1925808 0.1579529 0.2070189 0.1854905
```

It is interesting to consider the distribution of the tagwise dispersion estimates. As we can see from the output below, the tagwise dispersion estimates range from a minimum of 0.09 to a maximum of 0.97, and the common dispersion estimate lies in between the median and mean values for the tagwise dispersion estimates.

```
> summary(d$tagwise.dispersion)
```

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
0.08842	0.18550	0.19260	0.19930	0.20700	0.99000

```
> d$common.dispersion
```

```
[1] 0.1977094
```

### 5.5.2 Testing

Once we have an estimate of the common dispersion and/or estimates of the tagwise dispersions, we can proceed with testing procedures for determining differential expression using `exactTest`.

By default, `exactTest` uses the common dispersion, but by adding the argument `common.disp=FALSE`, tagwise dispersion estimates will be used instead.

```
> de.tagwise <- exactTest(d, common.disp = FALSE)
```

Comparison of groups: WT - DCLK

Just as we saw earlier, the object produced by `exactTest` contains two elements. The first is a data frame (`table`) that contains the elements `logConc`, `logFC` and `p.value` and the second is a vector (`comparison`) that lists the names of the groups being compared.

The output below shows that when using tagwise dispersions, the `edgeR` package still identifies a lot of differential expression between the wild-type group and the DCLK-transgenic group. The top DE tags are given very small  $p$ -values, even after adjusting for multiple testing. However, We see immediately that the  $p$ -values for the top tags are many orders of magnitude greater than those for the top tags identified using the common dispersion.

As with the analysis using the common dispersion, all of the top tags have a large fold change, indicating that these changes in expression are likely to be biologically meaningful, although interestingly we see more tags (7 out of 10) that are down-regulated in the wild-type group compared with the DCLK group, which contrasts with using the common dispersion. We note that the ranking of the tags is different, too, and only three of the top ten tags according to using the common dispersion are found to be among the top ten tags using tagwise dispersions.



```
> topTags(de.tagwise)
```

```
Comparison of groups: WT - DCLK
```

	logConc	logFC	PValue	FDR
TCTGTACGCAGTCAGGC	-18.46778	-9.732317	2.271105e-18	2.539300e-13
CATAAGTCACAGAGTCG	-32.76303	-34.506051	4.507171e-15	2.519711e-10
CCAAGAATCTGGTCGTA	-17.46762	-3.929366	1.966857e-12	7.330412e-08
AATTTCTTCCTCTTCCT	-17.30380	11.607564	3.139447e-12	8.775460e-08
ATACTGACATTTCTGTAT	-16.77800	4.144907	6.097301e-12	1.363466e-07
GCTAATAAATGGCAGAT	-14.91149	-3.295240	9.212532e-12	1.716740e-07
CTGCTAAGCAGAAGCAA	-16.99434	-3.427292	1.803488e-11	2.880660e-07
TTCCTGAAAATGTGAAG	-17.08403	-3.639794	2.653336e-11	3.708335e-07
AAAAGAAATCACAGTTG	-32.97330	-34.085504	6.032072e-11	7.493777e-07
AGTGTGACGTGACCGGG	-19.07157	8.035868	1.581782e-10	1.768575e-06

Of course, we can also rank the top tags using the fold change instead of the  $p$ -value. The results of doing this are shown in the table below, but this ranking is dominated by genes that have zero total counts in one group and is less informative than ranking by  $p$ -value.

```
> topTags(de.tagwise, n = 10, sort.by = "logFC")
```

```
Comparison of groups: WT - DCLK
```

	logConc	logFC	PValue	FDR
AAGACTCAGGACTCATC	-32.29053	35.45105	1.216554e-08	5.667572e-05
CCTGATGCTACAGAAAA	-32.75498	34.52215	4.898918e-07	1.165411e-03
CATAAGTCACAGAGTCG	-32.76303	-34.50605	4.507171e-15	2.519711e-10
ACTCTGTGTATTACTCC	-32.92486	34.18238	2.898915e-08	1.200463e-04
AAAAGAAATCACAGTTG	-32.97330	-34.08550	6.032072e-11	7.493777e-07
GATTTTTGTGCTGTTGG	-33.00084	34.03043	1.747407e-07	4.765265e-04
CACATAAGACTTTGGAC	-33.13007	33.77197	2.927280e-06	3.596662e-03
GAAATTCTCCATTGATT	-33.15363	33.72485	7.690677e-07	1.500202e-03
AAAATGTTGTTTATGGA	-33.15760	33.71690	5.539764e-06	5.567035e-03
AAATTATTCTCTTCCT	-33.18808	33.65595	1.494026e-06	2.456552e-03

The tables below shows the raw counts for the genes that **edgeR** has identified as the most differentially expressed, using the common dispersion and tagwise dispersions. For these tags, using both methods, there seem to be very large differences between the groups, suggesting that the DE genes identified are truly differentially expressed, and not false positives.

Particularly noteworthy, however, is how much more consistent the counts *within* groups are for the top tags identified using tagwise dispersions compared with those identified using the common dispersion. This is to be expected, as allowing tagwise dispersions penalises highly variable tags, so those that have greater variability within groups (especially one or two libraries with extremely high counts) will appear far lower in the ranking using tagwise dispersions than they would using the common dispersion. This difference in the rankings provided by the two approaches to the dispersion parameter could yield valuable information.

```
> detags.tgw <- rownames(topTags(de.tagwise)$table)
> detags.com <- rownames(topTags(de.common)$table)
> d$counts[detags.tgw, ]
```

	GSM272105	GSM272106	GSM272318	GSM272319	GSM272320
TCTGTACGCAGTCAGGC	160	0	101	1	440
CATAAGTCACAGAGTCG	67	0	77	0	58
CCAAGAATCTGGTCGTA	70	3	66	5	47
AATTTCTTCCTCTTCCT	1	44	0	1	0
ATACTGACATTTTCGTAT	5	113	5	228	8
GCTAATAAATGGCAGAT	387	45	321	32	132
CTGCTAAGCAGAAGCAA	76	7	88	7	52
TTCCTGAAAATGTGAAG	74	6	70	9	86
AAAAGAAATCACAGTTG	31	0	90	0	42
AGTGTGACGTGACCGGG	0	249	0	2	1
	GSM272321	GSM272322	GSM272323		
TCTGTACGCAGTCAGGC	0	33	0		
CATAAGTCACAGAGTCG	0	7	0		
CCAAGAATCTGGTCGTA	0	13	7		
AATTTCTTCCTCTTCCT	76	0	3487		
ATACTGACATTTTCGTAT	4	1	104		
GCTAATAAATGGCAGAT	1	71	38		
CTGCTAAGCAGAAGCAA	0	15	11		
TTCCTGAAAATGTGAAG	0	10	7		
AAAAGAAATCACAGTTG	0	3	0		
AGTGTGACGTGACCGGG	5	0	85		

```
> d$counts[detags.com, ]
```

	GSM272105	GSM272106	GSM272318	GSM272319	GSM272320
AATTTCTTCCTCTTCCT	1	44	0	1	0
CCGTCTTCTGCTTGTCG	106	1485	268	420	601
TCTGTACGCAGTCAGGC	160	0	101	1	440
CCGTCTTCTGCTTGTA	12	87	21	28	31
CCGTCTTCTGCTTGTC	2	42	8	17	19
AAGACTCAGGACTCATC	0	6	0	2	0
CCGTCTTCTGCTTGTA	9	61	11	20	17
AGTGTGACGTGACCGGG	0	249	0	2	1
AAATTCTTCCTCTTCCT	1	6	0	0	0
TGTGTATCCCACAAGGG	1	1	1	0	0
	GSM272321	GSM272322	GSM272323		
AATTTCTTCCTCTTCCT	76	0	3487		
CCGTCTTCTGCTTGTCG	5156	5	242		

TCTGTACGCAGTCAGGC	0	33	0
CCGTCTTCTGCTTGTA	352	1	14
CCGTCTTCTGCTTGCA	183	1	17
AAGACTCAGGACTCATC	4	0	461
CCGTCTTCTGCTTGTA	133	0	9
AGTGTGACGTGACCGGG	5	0	85
AAATTCTTCCTCTTCCT	2	0	288
TGTGTATCCCACAAGGG	6	0	252

We might also be interested in comparing the top-ranking genes as identified by **edgeR** using the common dispersion and tagwise dispersions. The output below shows, firstly, that there are three tags that appear in the top ten most DE tags using both common and tagwise dispersions. Secondly, we see that of the top 1000 most DE tags as identified using tagwise dispersions, 77% of these tags are also in the list of the 1000 most DE tags as identified using the common dispersion. This shows that although we do get quite different results depending on which method we use, there is still a great deal of agreement as to which tags are DE.

```
> sum(rownames(topTags(de.tagwise)$table) %in% rownames(topTags(de.common)$table))

[1] 3

> sum(rownames(topTags(de.tagwise, n = 1000)$table) %in% rownames(topTags(de.common,
+   n = 1000)$table))/1000 * 100

[1] 76.7
```

Using their dedicated Bayesian model, 't Hoen et al. [2008] found 3179 transcripts to be differentially expressed with a FDR of 8.5%. The output below shows that using Benjamini and Hochberg [1995]'s approach for controlling the FDR at 8.5%, **edgeR** identifies 1717 tags as DE using common dispersion and 1441 tags as DE using tagwise dispersions. This means that we determine 1.54% and 1.29% of tags to be DE using common and tagwise dispersions, respectively.

```
> sum(p.adjust(de.common$table$p.value, method = "BH") < 0.085)

[1] 1710

> mean(p.adjust(de.common$table$p.value, method = "BH") <
+   0.085) * 100

[1] 1.529394

> sum(p.adjust(de.tagwise$table$p.value, method = "BH") <
+   0.085)
```

```
[1] 1441
```

```
> mean(p.adjust(de.tagwise$table$p.value, method = "BH") <
+       0.085) * 100
```

```
[1] 1.288805
```

Of the 1441 tags identified as DE using tagwise dispersions, 729 (51%) are up-regulated in wild-type and 712 (49%) are up-regulated in the transgenic mice. The proportions of up- and down-regulated genes identified using the two approaches to modeling the dispersion are similar, but using the common dispersion identifies slightly more tags up-regulated in wild-type mice as DE.

```
> top.tgw <- topTags(de.tagwise, n = 1441)
> sum(top.tgw$table$logFC > 0)
```

```
[1] 729
```

```
> sum(top.tgw$table$logFC < 0)
```

```
[1] 712
```

### 5.5.3 Visualising DGE results

As discussed earlier, the function `plotSmear` can be used to generate a plot of the log-fold change against the log-concentration for each tag (analogous to an MA-plot in the microarray context). We identify the top 500 most DE tags using both common dispersion and tagwise dispersions so we can highlight them on the plots and compare what we see. The code for producing the fold-change plots is shown below, and the result of this code is shown in Figure 6.

```
> detags500.com <- rownames(topTags(de.common, n = 500)$table)
> detags500.tgw <- rownames(topTags(de.tagwise, n = 500)$table)

> par(mfcol = c(2, 1))
> plotSmear(d, de.tags = detags500.com, main = "Using common dispersion")
> abline(h = c(-2, 2), col = "dodgerblue", lwd = 2)
> plotSmear(d, de.tags = detags500.tgw, main = "Using tagwise dispersions")
> abline(h = c(-2, 2), col = "dodgerblue", lwd = 2)
```

In Figure 6, the top 500 most differentially expressed tags (those identified as significant by `edgeR` using the common dispersion (top) and tagwise dispersions (bottom)) are highlighted in red. Looking at Figure 6, we see that, generally speaking, the pattern of differential expression looks similar using the two different methods, and the tags identified as DE have convincingly large fold changes.

## 5.6 Setup

This analysis of 't Hoen et al. [2008]'s tag-based DGE data was conducted on:

```
> sessionInfo()

R version 2.9.1 (2009-06-26)
i386-apple-darwin8.11.1

locale:
en_AU.UTF-8/en_AU.UTF-8/C/C/en_AU.UTF-8/en_AU.UTF-8

attached base packages:
[1] stats      graphics  grDevices  utils      datasets  methods   base

other attached packages:
[1] edgeR_1.3.6

loaded via a namespace (and not attached):
[1] limma_2.18.2
```

and took 5–10 minutes to carry out on an Apple MacBook with a 2.4 Ghz Intel Core 2 Duo processor and 4 Gb of 1067 MHz DDR3 memory.

## 6 Case Study: RNA-seq data

### 6.1 Introduction

This section provides a detailed analysis of data from a study by Li et al. [2008] designed to address a range of practical issues in RNA-seq experiments:

1. How many annotated genes are detected in a single cell type?
2. What is the number of tags that is necessary for the analysis of differentially regulated genes under different experimental conditions?
3. To what extent can different mRNA isoforms be detected?
4. How can one quantify alternative splicing by using a single or combination of existing technologies?

Li et al. [2008] attempt to address all of these issues on an androgen-sensitive prostate cancer cell model. We are interested primarily in the second question, and the challenge of identifying differentially regulated genes under different experimental conditions. We will demonstrate the use of the **edgeR** package for analyzing RNA-seq data for differential gene expression.

## 6.2 Source of the data

Li et al. [2008] sequenced poly(A)<sup>+</sup> RNA from mock-treated or androgen sensitive LNCaP cells (a cell line of human cells commonly used in the field of oncology) on the Illumina 1G Genome Analyzer. The researchers used a double-random priming approach that was capable of generating strand-specific information, although this is not of relevance to our analysis here. The raw RNA-seq data provided by Li et al. consists of 7 ‘lanes’ of 35bp reads.<sup>1</sup> Approximately 10 million sequence tags were generated from both control and hormone-treated cells (treated with DHT), and Li et al. [2008]’s analysis suggests that this tag density is sufficient for quantitative analysis of gene expression.

The 10 million sequenced tags arise from four libraries from control cells and three libraries for hormone-treated cells, giving a total of seven libraries to analyse. From Li et al. [2008] and its companion paper [Li et al., 2006] it is unclear as to whether the treatments are independent or not. The following analysis shows how a quantitative analysis of gene expression, focusing on identifying differentially expressed genes, can be conducted for these seven libraries using **edgeR**.

## 6.3 Reading in the data and creating a DGEList object

Our first task is to load the **edgeR** package and read the data into R. In this case, the tag counts for the libraries are stored in a single table in a plain text file `pnas_expression.txt`, in which the rows of the table represent tags and the columns represent the different libraries.

To turn the raw RNA-seq data into a table of counts, reads were mapped to the NCBI36 build of the human genome using **bowtie**, allowing up to two mismatches. Reads which did not map uniquely were discarded. The number of mapped reads that overlapped ENSEMBL gene annotations (version 53) was then counted. In counting reads associated with genes, reads which mapped to non-coding gene regions, such as introns, were included in the count.

Unlike in the other datasets we have look at, counts here are aggregated at the gene, not at the tag, level.

The `files` object provides the name of the data file, and makes a convenient argument to the function `read.delim` which reads the table of counts into our R session.

```
> setwd("/Users/davismcc/Documents/Honours/Data/LiData")
> library(edgeR)
> raw.data <- read.delim("pnas_expression.txt")
> names(raw.data)
```

[1]	"ensembl_ID"	"lane1"	"lane2"	"lane3"	"lane4"
[6]	"lane5"	"lane6"	"lane8"	"len"	

The raw data is stored in a table with columns representing the gene names, the counts for the seven libraries and a column giving the length of each gene. The gene length is not currently used

---

<sup>1</sup>The Illumina instrument requires samples to be placed in a ‘flow cell’ which contains eight ‘lanes’—each lane has a sample of cDNA and generates a library of sequence counts for that sample.

by `edgeR`, but this information could be used in future versions of the package. In the code below, we assign the counts matrix to an object `d` with the appropriate rownames, define the groups to which the samples belong, and then pass these arguments to `DGEList`, which calculates the library sizes and constructs a `DGEList` containing all of the data we require for the analysis.

```
> d <- raw.data[, 2:8]
> rownames(d) <- raw.data[, 1]
> group <- c(rep("Control", 4), rep("DHT", 3))
> d <- DGEList(counts = d, group = group)
> d
```

An object of class "DGEList"

```
$samples
      group lib.size
lane1 Control  978576
lane2 Control 1156844
lane3 Control 1442169
lane4 Control 1485604
lane5      DHT 1823460
lane6      DHT 1834335
lane8      DHT  681743
```

```
$counts
      lane1 lane2 lane3 lane4 lane5 lane6 lane8
ENSG00000124208  478  619  628  744  483  716  240
ENSG00000182463   27   20   27   26   48   55   24
ENSG00000124201  180  218  293  275  373  301   88
ENSG00000124205    0    0    5    5    0    0    0
ENSG00000124207   76   80   85   97   80   81   37
21872 more rows ...
```

This `DGEList` is now ready to be passed to the functions that do the calculations to determine differential expression levels for the genes.

## 6.4 Analysis using common dispersion

### 6.4.1 Estimating the common dispersion

As discussed for the SAGE data, the first major step in the analysis of DGE data using the NB model is to estimate the dispersion parameter for each tag. Like in the earlier case study, we begin by estimating the common dispersion using the function `estimateCommonDisp`, and analysing the data using the common dispersion.

```
> d <- estimateCommonDisp(d)
> names(d)

[1] "samples"          "common.dispersion" "counts"
[4] "pseudo.alt"       "conc"              "common.lib.size"

> d
```

An object of class "DGEList"

```
$samples
      group lib.size
lane1 Control  978576
lane2 Control 1156844
lane3 Control 1442169
lane4 Control 1485604
lane5   DHT  1823460
lane6   DHT  1834335
lane8   DHT   681743
```

```
$common.dispersion
[1] 0.02021596
```

```
$counts
      lane1 lane2 lane3 lane4 lane5 lane6 lane8
ENSG00000124208  478  619  628  744  483  716  240
ENSG00000182463   27   20   27   26   48   55   24
ENSG00000124201  180  218  293  275  373  301   88
ENSG00000124205    0    0    5    5    0    0    0
ENSG00000124207   76   80   85   97   80   81   37
21872 more rows ...
```

```
$pseudo.alt
      lane1      lane2      lane3      lane4      lane5
ENSG00000124208 623.7011345 682.94207324 555.660542 639.479771 336.71526
ENSG00000182463  34.3356362  22.18976707  23.832567  22.180621  33.16394
ENSG00000124201 235.0851553 240.62900197 259.559061 236.246548 262.61397
ENSG00000124205  0.1502441  0.05777303  4.539068  4.427231  0.00000
ENSG00000124207  98.4667235  88.25763482  75.005547  83.279817  55.73657
      lane6      lane8
ENSG00000124208 499.57554 4.485689e+02
ENSG00000182463  38.29654 4.367427e+01
ENSG00000124201 209.30644 1.685512e+02
ENSG00000124205  0.00000 1.509887e-10
```



```

ENSG00000124207 56.12481 6.774033e+01
21872 more rows ...

$conc
$conc.common
ENSG00000124208 ENSG00000182463 ENSG00000124201 ENSG00000124205
  4.236152e-04    2.419602e-05    1.809021e-04    1.063407e-06
ENSG00000124207
  5.831078e-05
21872 more elements ...

$conc.group
          Control          DHT
ENSG00000124208 4.897757e-04 3.350953e-04
ENSG00000182463 1.990269e-05 2.966863e-05
ENSG00000124201 1.902894e-04 1.684999e-04
ENSG00000124205 1.963536e-06 8.783496e-16
ENSG00000124207 6.735245e-05 4.640575e-05
21872 more rows ...

$common.lib.size
[1] 1276768

```

The output of `estimateCommonDisp` is a `DGEList` object with several new elements. The element `common.dispersion`, as the name suggests, provides the estimate of the common dispersion. The pseudocounts calculated under the alternative hypothesis are given by `pseudo.alt`. The element `conc` gives the estimates of the overall concentration of each tag across all of the original samples (`conc$conc.common`) and the estimate of the concentration of each tag within each group (`conc$conc.group`). The element `common.lib.size` gives the library size to which the original libraries have been adjusted in the pseudocounts.

We see in the output below that the total counts in each library of the pseudocounts agrees well with the common library size, as desired.

```

> d$samples$lib.size

[1] 978576 1156844 1442169 1485604 1823460 1834335 681743

> d$common.lib.size

[1] 1276768

> colSums(d$pseudo.alt)

```

```

lane1 lane2 lane3 lane4 lane5 lane6 lane8
1277021 1276791 1276935 1277035 1277209 1277069 1277919

```

Here the coefficient of variation of biological variation (square root of the common dispersion) is found to be 0.142. We also note that although a common dispersion estimate of 0.02 may seem ‘small’, if a tag has just 200 counts, then the estimate of the tag’s variance is 5 times greater than it would be under the Poisson model.

```

> d$common.dispersion

[1] 0.02021596

> sqrt(d$common.dispersion)

[1] 0.1421828

```

### 6.4.2 Testing

Once we have an estimate of the common dispersion, we can proceed with testing procedures for determining differential expression. As for the SAGE data, there are only two groups here, so the pair need not be specified in the call to `exactTest`.

```

> de.com <- exactTest(d)

Comparison of groups: DHT - Control

> names(de.com)

[1] "table"      "comparison"

```

The results of the NB exact test can be accessed conveniently using the `topTags` function applied to the object produced by `exactTest`. The table below shows the top 10 DE genes ranked by  $p$ -value.

The table in the output from `topTags` shows that the `edgeR` package identifies a great deal of differential expression, and gives the top genes extremely small  $p$ -values, even after adjusting for multiple testing. Furthermore, all of the top genes have a very large fold change (indicating that these tags are likely to be biologically meaningful), and all are up-regulated in the DHT-treatment group compared to the control group.

Of course, for many applications the ranking for differential expression is more important than the  $p$ -value, and `topTags` provides such a ranking. As suggested in the SAGE case study, a Gene Ontology analysis could be carried out using the list of top gene and  $p$ -values provided by `topTags` in order to obtain more systematic and functional information about the differentially expressed genes.

```
> topTags(de.com)
```

```
Comparison of groups: DHT - Control
```

	logConc	logFC	PValue	FDR
ENSG00000151503	-11.94799	5.705233	7.744047e-185	1.694165e-180
ENSG00000096060	-11.33288	4.893134	5.349073e-155	5.851083e-151
ENSG00000127954	-15.63280	8.118692	7.331162e-148	5.346128e-144
ENSG00000166451	-12.28742	4.570439	7.122773e-128	3.895623e-124
ENSG00000131016	-14.42856	5.190737	1.701099e-104	7.442990e-101
ENSG00000113594	-12.83343	4.000650	2.579172e-96	9.404091e-93
ENSG00000116285	-13.56732	4.087861	8.108902e-88	2.534264e-84
ENSG00000123983	-12.09539	3.544802	1.444749e-86	3.950846e-83
ENSG00000166086	-15.24551	5.390848	6.219612e-86	1.511849e-82
ENSG00000162772	-10.81704	3.201950	7.560702e-80	1.654055e-76

The table below shows the raw counts for the genes that `edgeR` has identified as the most differentially expressed. For these genes there seems to be very large differences between the groups, suggesting that the DE genes identified are truly differentially expressed.

```
> detags.com <- rownames(topTags(de.com)$table)
> d$counts[detags.com, ]
```

	lane1	lane2	lane3	lane4	lane5	lane6	lane8
ENSG00000151503	35	35	49	59	3307	3439	1224
ENSG00000096060	65	79	105	113	3975	3727	1451
ENSG00000127954	0	0	3	3	607	602	220
ENSG00000166451	41	52	57	57	1750	1654	728
ENSG00000131016	9	5	18	6	564	377	213
ENSG00000113594	37	36	57	43	936	959	418
ENSG00000116285	18	28	23	32	645	630	218
ENSG00000123983	62	76	94	108	1354	1258	628
ENSG00000166086	9	2	3	6	296	298	121
ENSG00000162772	172	204	250	304	2972	3269	1112

If we order the genes by fold change instead of  $p$ -value, we see that the genes with the largest fold changes have very small concentrations. This ranking is dominated by genes that have zero total counts in one group and is less informative than ranking by  $p$ -value.

```
> topTags(de.com, n = 10, sort.by = "logFC")
```

```
Comparison of groups: DHT - Control
```

	logConc	logFC	PValue	FDR
ENSG00000091972	-31.75811	-36.51589	8.689939e-56	6.789635e-53

```

ENSG00000164120 -32.27738 35.47735 4.636882e-44 2.205241e-41
ENSG00000100373 -32.93100 -34.17010 2.739292e-17 2.147939e-15
ENSG00000118513 -33.00607 -34.01998 8.893707e-16 5.895989e-14
ENSG00000081237 -33.15786 -33.71640 5.634630e-13 2.691459e-11
ENSG00000196660 -33.22302 -33.58606 3.870150e-12 1.647223e-10
ENSG00000117245 -33.23863 -33.55484 1.051358e-11 4.151725e-10
ENSG00000019549 -33.39510 33.24191 2.420329e-13 1.225684e-11
ENSG00000137404 -33.41447 -33.20316 1.041329e-08 2.556807e-07
ENSG00000059804 -33.43964 33.15284 2.174556e-12 9.630115e-11

```

We can see how many genes are identified as differentially expressed between the control group (untreated LNCaP cells) and the DHT-treated LNCaP cells, for a given threshold for the exact  $p$ -value or for the adjusted  $p$ -value.

As the output below shows, **edgeR** detects a huge number of differentially expressed genes in this dataset. Almost 5000 genes are given a  $p$ -value less than 0.01.

```
> sum(de.com$table$p.value < 0.01)
```

```
[1] 4760
```

The output below shows that over 4835 genes are given an adjusted  $p$ -value of less than 0.05. This means that if we set our control the FDR for differential expression at 5%, then **edgeR** identifies 22% of all the genes in the dataset as differentially expressed.

```
> sum(p.adjust(de.com$table$p.value, method = "BH") < 0.05)
```

```
[1] 4835
```

```
> mean(p.adjust(de.com$table$p.value, method = "BH") < 0.05) *
+      100
```

```
[1] 22.10084
```

Of the genes identified as DE above, 1911 (40% of the DE genes) are up-regulated in DHT-treated compared with control cells, and 2924 (60%) are up-regulated in the control cells compared with DHT-treated cells. It is interesting to note that although we detect far more genes as DE that are up-regulated in the control group, all of the top ten genes were up-regulated in the DHT-treated group.

```
> top.com <- topTags(de.com, n = 4835)
> sum(top.com$table$logFC > 0)
```

```
[1] 1911
```

```
> sum(top.com$table$logFC < 0)
```

```
[1] 2924
```

### 6.4.3 Visualising DGE results

The code for producing the default fold-change plot, with the top 500 most DE tags highlighted in red, is shown below, and the result of this code is shown in Figure 5. In Figure 5, we see that the 500 tags identified as most differentially expressed have large fold changes—almost all of the 500 tags in red fall outside the blue lines at  $\log FC = -2$  and  $\log FC = 2$ . This means that most of these tags show at least a 4-fold change in expression level between the samples. This plot suggests strongly that the tags identified by **edgeR** as differentially expressed are truly differentially expressed, and, given the large changes in expression level, are likely to be biologically meaningful.

```
> detags500.com <- rownames(topTags(de.com, n = 500)$table)

> plotSmear(d, de.tags = detags500.com, main = "FC plot using common dispersion")
> abline(h = c(-2, 2), col = "dodgerblue", lwd = 2)
```

## 6.5 Analysis using moderated tagwise dispersions

### 6.5.1 Estimating the tagwise dispersion

As discussed in the previous case studies, an extension to simply using the common dispersion for each tag is to estimate the dispersion separately for each tag, while ‘squeezing’ these estimates towards the common dispersion estimate. The goal of this moderation of the dispersion estimates is to improve inference by sharing information between tags. This type of analysis can be carried out in few steps using the **edgeR** package.

To run the moderated analysis, we need to determine how much moderation is necessary. As discussed in the SAGE case study, we can use an empirical Bayes rule that involves calculating a weight parameter `prior.n`. However, for many applications (especially if the estimated smoothing parameter is large), using the common dispersion for all tags will give excellent results.

The smoothing parameter, `prior.n` can then be calculated using the function **estimateSmoothing**, which takes the **DGEList** object produced by **estimateCommonDisp** as its argument. As we see below, for this dataset the estimate of the smoothing parameter is very small, so if we were to use this tiny value for the weight parameter we would moderate the tagwise dispersion estimates so little that it would be equivalent to using just using the tagwise dispersion for each gene without any ‘squeezing’ at all towards the common dispersion.

```
> prior.n <- estimateSmoothing(d)
> prior.n
```

```
[1] 0.0008377133
```

As we only have seven libraries, a small sample size, we should not be too confident about the accuracy of the tagwise dispersions. Therefore it is recommended to use a larger value for `prior.n`, which can be selected *a priori*, instead of being estimated. In an experiment such as that

we consider here, in which we have seven samples and thus five degrees of freedom for estimating the dispersion parameter, setting the `prior.n` to be ten should be appropriate. This means that the common likelihood receives the weight of ten individual tags, so there will be a reasonable degree of ‘squeezing’ towards the common dispersion estimate, but there is still enough scope to allow flexibility with the individual dispersion for each gene.

The function `estimateTagwiseDisp` produces a `DGEList` object that contains all of the elements present in the object produced by `estimateCommonDisp`, as well as the value for `prior.n` used (`d$prior.n`) and the tagwise dispersion estimates (`d$tagwise.dispersion`), as we see below. Here we set `grid.length=500` for greater precision in the tagwise dispersion estimates.

```
> d <- estimateTagwiseDisp(d, prior.n = 10, grid.length = 500)
```

Using grid search to estimate tagwise dispersion.

```
> names(d)
```

```
[1] "samples"           "common.dispersion" "prior.n"
[4] "tagwise.dispersion" "counts"           "pseudo.alt"
[7] "conc"              "common.lib.size"
```

```
> d$prior.n
```

```
[1] 10
```

```
> head(d$tagwise.dispersion)
```

```
[1] 0.01936799 0.01729400 0.01936799 0.02145046 0.01522843 0.02774923
```

It is interesting to consider the distribution of the tagwise dispersion estimates. As we can see from the output below, the tagwise dispersion estimates range from a minimum of 0.005 to a maximum of 0.236, and the common dispersion estimate lies in between the median and mean values for the tagwise dispersion estimates.

```
> summary(d$tagwise.dispersion)
```

```
      Min.   1st Qu.   Median     Mean   3rd Qu.     Max.
0.005025 0.019370 0.019370 0.020640 0.021450 0.236100
```

```
> d$common.dispersion
```

```
[1] 0.02021596
```

### 6.5.2 Testing

Once we have an estimate of the common dispersion and/or estimates of the tagwise dispersions, we can proceed with testing procedures for determining differential expression using `exactTest`.

By default, `exactTest` uses the common dispersion, but by adding the argument `common.disp=FALSE`, tagwise dispersion estimates will be used instead.

```
> de.tgw <- exactTest(d, common.disp = FALSE)
```

Comparison of groups: DHT - Control

The output below shows that when using tagwise dispersions, the `edgeR` package still identifies a huge amount of differential expression between the control group and the DHT-treated group. The top DE tags are given even smaller  $p$ -values than using the common dispersion—many, many orders of magnitude smaller.

As with the analysis using the common dispersion, all of the top genes have large fold change, indicating that these changes in expression are likely to be biologically meaningful. Again, all of the top genes are up-regulated in the DHT-treated group compared with the control group. We note that the ranking of the tags is similar, with seven of the top ten genes using the common dispersion to be found among the top ten genes using tagwise dispersions.

```
> topTags(de.tgw)
```

Comparison of groups: DHT - Control

	logConc	logFC	PValue	FDR
ENSG00000151503	-11.947221	5.704024	2.214558e-301	4.844788e-297
ENSG00000096060	-11.332026	4.891305	1.545034e-259	1.690035e-255
ENSG00000166451	-12.288475	4.570589	8.545084e-180	6.231360e-176
ENSG00000127954	-15.632016	8.117608	5.274185e-171	2.884584e-167
ENSG00000162772	-10.816415	3.201287	6.821241e-136	2.984566e-132
ENSG00000113594	-12.834292	3.999954	8.573960e-119	3.126209e-115
ENSG00000116133	-11.741194	3.128433	2.367018e-118	7.397607e-115
ENSG00000116285	-13.566933	4.089714	4.303139e-116	1.176747e-112
ENSG00000115648	-8.831597	2.481756	1.967977e-114	4.783715e-111
ENSG00000130066	-10.322217	2.494893	6.742514e-108	1.475060e-104

Of course, we can also rank the top tags using the fold change instead of the  $p$ -value, as described above, this ranking is dominated by genes that have zero total counts in one group and is less informative than ranking by  $p$ -value.

```
> topTags(de.tgw, n = 10, sort.by = "logFC")
```

Comparison of groups: DHT - Control

	logConc	logFC	PValue	FDR
ENSG00000091972	-31.75810	-36.51592	2.059993e-63	1.502216e-60
ENSG00000164120	-32.27722	35.47767	1.732888e-44	5.123027e-42
ENSG00000100373	-32.93097	-34.17017	1.170463e-17	7.759461e-16
ENSG00000118513	-33.00748	-34.01715	6.961165e-15	3.696345e-13
ENSG00000081237	-33.15838	-33.71535	1.283161e-12	5.113246e-11
ENSG00000196660	-33.22317	-33.58577	3.427356e-12	1.288321e-10
ENSG00000117245	-33.23845	-33.55521	1.635293e-11	5.651708e-10
ENSG00000019549	-33.39438	33.24334	2.743940e-13	1.175645e-11
ENSG00000059804	-33.43993	33.15225	2.018339e-12	7.801273e-11
ENSG00000137404	-33.44594	-33.14022	5.612659e-07	9.183854e-06

The tables below shows the quantile-adjusted counts (i.e. counts for equalised library sizes) for the genes that **edgeR** has identified as the most differentially expressed, using the common dispersion and tagwise dispersions. For these tags, using both methods, there seem to be very large differences between the groups, suggesting that the DE genes identified are truly differentially expressed, and not false positives.

We saw for 't Hoen et al. [2008]'s data how much more consistent the counts *within* groups are for the top tags identified using tagwise dispersions compared with those identified using the common dispersion. This effect is not nearly as pronounced here.

```
> detags.tgw <- rownames(topTags(de.tgw)$table)
> detags.com <- rownames(topTags(de.com)$table)
> round(d$pseudo.alt[detags.tgw, ])
```

	lane1	lane2	lane3	lane4	lane5	lane6	lane8
ENSG00000151503	46	39	43	51	2315	2394	2293
ENSG00000096060	85	87	93	97	2783	2594	2717
ENSG00000166451	53	57	50	49	1225	1151	1361
ENSG00000127954	0	0	3	3	425	419	412
ENSG00000162772	225	225	221	262	2081	2276	2083
ENSG00000113594	48	40	51	37	655	667	780
ENSG00000116133	127	118	137	123	1143	1121	1041
ENSG00000116285	24	31	20	28	452	439	409
ENSG00000115648	1226	1196	1166	1156	6813	6920	6130
ENSG00000130066	403	426	440	410	2239	2301	2571

```
> round(d$pseudo.alt[detags.com, ])
```

	lane1	lane2	lane3	lane4	lane5	lane6	lane8
ENSG00000151503	46	39	43	51	2315	2394	2293
ENSG00000096060	85	87	93	97	2783	2594	2717



ENSG00000127954	0	0	3	3	425	419	412
ENSG00000166451	53	57	50	49	1225	1151	1361
ENSG00000131016	12	6	16	5	396	261	396
ENSG00000113594	48	40	51	37	655	667	780
ENSG00000116285	24	31	20	28	452	439	409
ENSG00000123983	81	84	83	93	948	875	1172
ENSG00000166086	11	2	3	5	207	207	226
ENSG00000162772	225	225	221	262	2081	2276	2083

We might also be interested in comparing the top-ranking genes as identified by **edgeR** using the common dispersion and tagwise dispersions. We see in the output below that of the top 1000 most DE tags as identified using tagwise dispersions, 87% of these tags are also in the list of the 1000 most DE tags as identified using the common dispersion. This shows that for this dataset there is a great deal of agreement between the common and tagwise dispersion approaches as to which tags are DE.

```
> sum(rownames(topTags(de.tgw, n = 1000)$table) %in% rownames(topTags(de.com,
+      n = 1000)$table))/1000 * 100
```

```
[1] 87.3
```

Using the common dispersion we found that 4835 genes (22% of the total number) are given an adjusted  $p$ -value of less than 0.05. In the output below, we see that using tagwise dispersions we obtain slightly more DE genes, namely 4933, or 23% of all of the genes in the dataset.

```
> sum(p.adjust(de.tgw$table$p.value, method = "BH") < 0.05)
```

```
[1] 4933
```

```
> mean(p.adjust(de.tgw$table$p.value, method = "BH") < 0.05) *
+      100
```

```
[1] 22.54880
```

Of the 4933 tags identified as DE using tagwise dispersions, 1981 (40%) are up-regulated in DHT-treated cells and 2952 (60%) are up-regulated in the control cells. The proportions of up- and down-regulated genes identified using the two approaches to modeling the dispersion are equal.

```
> top.tgw <- topTags(de.tgw, n = 4933)
> sum(top.tgw$table$logFC > 0)
```

```
[1] 1981
```

```
> sum(top.tgw$table$logFC < 0)
```

```
[1] 2952
```

### 6.5.3 Visualising DGE results

As discussed earlier, the function `plotSmear` can be used to generate a plot of the log-fold change against the log-concentration for each tag. We identify the top 500 most DE tags using both common dispersion and tagwise dispersions so we can highlight them on the plots and compare what we see. The code for producing the fold-change plots (in the one frame for purposes of comparison) is shown below, and the result of this code is shown in Figure 6.

```
> detags500.com <- rownames(topTags(de.com, n = 500)$table)
> detags500.tgw <- rownames(topTags(de.tgw, n = 500)$table)

> par(mfcol = c(2, 1))
> plotSmear(d, de.tags = detags500.com, main = "Using common dispersion")
> abline(h = c(-2, 2), col = "dodgerblue", lwd = 2)
> plotSmear(d, de.tags = detags500.tgw, main = "Using tagwise dispersions")
> abline(h = c(-2, 2), col = "dodgerblue", lwd = 2)
```

In Figure 6, the top 500 most differentially expressed genes (those identified as significant by `edgeR` using the common dispersion (top) and tagwise dispersions (bottom)) are highlighted in red. Looking at Figure 6, we see that, generally speaking, the pattern of differential expression looks similar using the two different methods, and the genes identified as DE have convincingly large fold changes.

## 6.6 Setup

This analysis of Li et al. [2008]’s RNA-seq data was conducted on:

```
> sessionInfo()

R version 2.9.1 (2009-06-26)
i386-apple-darwin8.11.1

locale:
en_AU.UTF-8/en_AU.UTF-8/C/C/en_AU.UTF-8/en_AU.UTF-8

attached base packages:
[1] stats      graphics  grDevices  utils      datasets  methods   base

other attached packages:
[1] edgeR_1.3.6

loaded via a namespace (and not attached):
[1] limma_2.18.2
```

and took 2–4 minutes to carry out on an Apple MacBook with a 2.4 Ghz Intel Core 2 Duo processor and 4 Gb of 1067 MHz DDR3 memory.

## 7 Poisson example

It has been noted that, in some deep sequencing approaches, not a great deal of overdispersion is observed. Specifically, the means and variances appear to be very close to each other, suggesting the Poisson distribution is a good fit. Methods within the **edgeR** package may still be useful, including the quantile adjustment (effectively a normalization) and the exact testing routines.

To illustrate this, we sample Poisson data and run **de4DGE** with the **doPoisson** argument set to **TRUE**. The data is quantile-adjusted and before the exact test is invoked, the dispersion parameter is set to 0. Currently, elements from the output of **de4DGE** must be manually added to the **DGEList** object, as **exactTest** operates only on **DGEList** objects, as illustrated in the case studies above.

Nevertheless, an analysis using the Poisson distribution can be carried out as follows:

```
> set.seed(101)
> n <- 10000
> lib.sizes <- c(40000, 50000, 38000, 40000)
> p <- runif(n, min = 1e-04, 0.001)
> mu <- outer(p, lib.sizes)
> mu[1:5, 3:4] <- mu[1:5, 3:4] * 8
> y <- matrix(rpois(4 * n, lambda = mu), nrow = n)
> dP <- DGEList(counts = y, group = rep(1:2, each = 2), lib.size = lib.sizes)
> msP <- de4DGE(dP, doPoisson = TRUE)
```

Quantile adjusting as Poisson.

```
> dP$pseudo.alt <- msP$pseudo
> dP$common.dispersion <- 1e-06
> dP$conc <- msP$conc
> dP$common.lib.size <- msP$M
```

And you can proceed as before:

```
> de.P <- exactTest(dP)
```

Comparison of groups: 2 - 1

```
> topTags(de.P)
```

Comparison of groups: 2 - 1

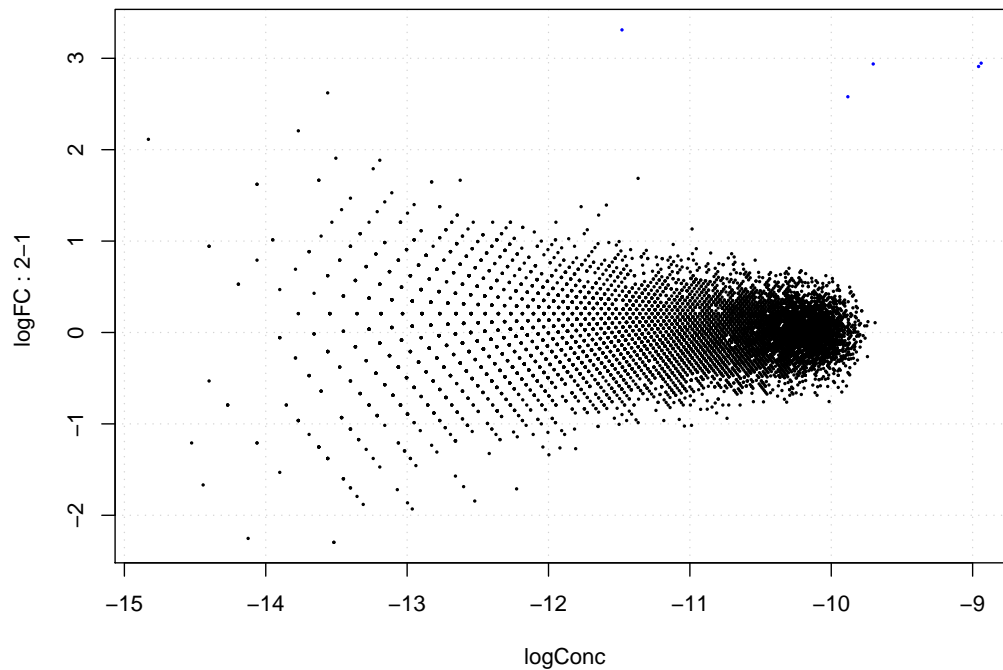
	logConc	logFC	PValue	FDR
3	-8.939897	2.946691	3.076540e-81	3.076540e-77
4	-8.958118	2.910250	1.425021e-77	7.125106e-74
1	-9.703306	2.937857	1.635095e-47	5.450317e-44
5	-9.882605	2.579261	2.030845e-33	5.077113e-30
2	-11.480315	3.310787	6.058052e-18	1.211610e-14

```

9796 -11.366488  1.686444 3.397842e-06 5.663070e-03
2893 -10.984522  1.132451 3.740766e-04 4.471809e-01
142  -11.590674  1.394078 3.940818e-04 4.471809e-01
3541 -13.561931  2.621489 4.024628e-04 4.471809e-01
9783 -12.225718 -1.711087 6.061462e-04 6.061462e-01

```

```
> plotSmear(dP, col = c(rep("blue", 5), rep("black", n - 5)))
```



## 8 Future improvements and extension

Here, we list some improvements/extensions that are planned for the **edgeR** package:

1. As the packages for the processing of raw high-throughput sequencing data become more mature, **edgeR** may need to adapt and operate on different objects. As shown above, **edgeR** operates on a simple object containing simple data summaries which will presumably be readily available from pre-processing steps.
2. Significant speed improvements have been made since the earlier versions of **edgeR**, but as the datasets become larger, some further optimizations may be necessary. We are exploring various ways to do this.

3. The current quantile-based normalization assumes the library sizes are fixed. Depending on the circumstances of the samples in question, it may be necessary to explore something like an *effective* library size.
4. We are exploring more general testing procedures.

## 9 Setup

This vignette was built on:

```
> sessionInfo()
```

```
R version 2.10.1 (2009-12-14)  
i386-pc-mingw32
```

```
locale:
```

```
[1] LC_COLLATE=English_United States.1252  
[2] LC_CTYPE=English_United States.1252  
[3] LC_MONETARY=English_United States.1252  
[4] LC_NUMERIC=C  
[5] LC_TIME=English_United States.1252
```

```
attached base packages:
```

```
[1] tools      stats      graphics  grDevices  utils      datasets  methods  
[8] base
```

```
other attached packages:
```

```
[1] edgeR_1.4.7
```

```
loaded via a namespace (and not attached):
```

```
[1] limma_3.2.1
```

## References

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- H. R. Li, M. T. Lovci, Y.-S. Kwon, M. G. Rosenfeld, X.-D. Fua, and G. W. Yeo. Determination of tag density required for digital transcriptome analysis: Application to an androgen-sensitive prostate cancer model. *Proceedings of the National Academy of Sciences of the USA*, 105(51): 20179–20184, 2008.
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- L. Zhang, W. Zhou, V. E. Velculescu, S. E. Kern, R. H. Hruban, S. R. Hamilton, B. Vogelstein, and K. W. Kinzler. Gene expression profiles in normal and cancer cells. *Science*, 276(5316): 1268–1272, May 1997.

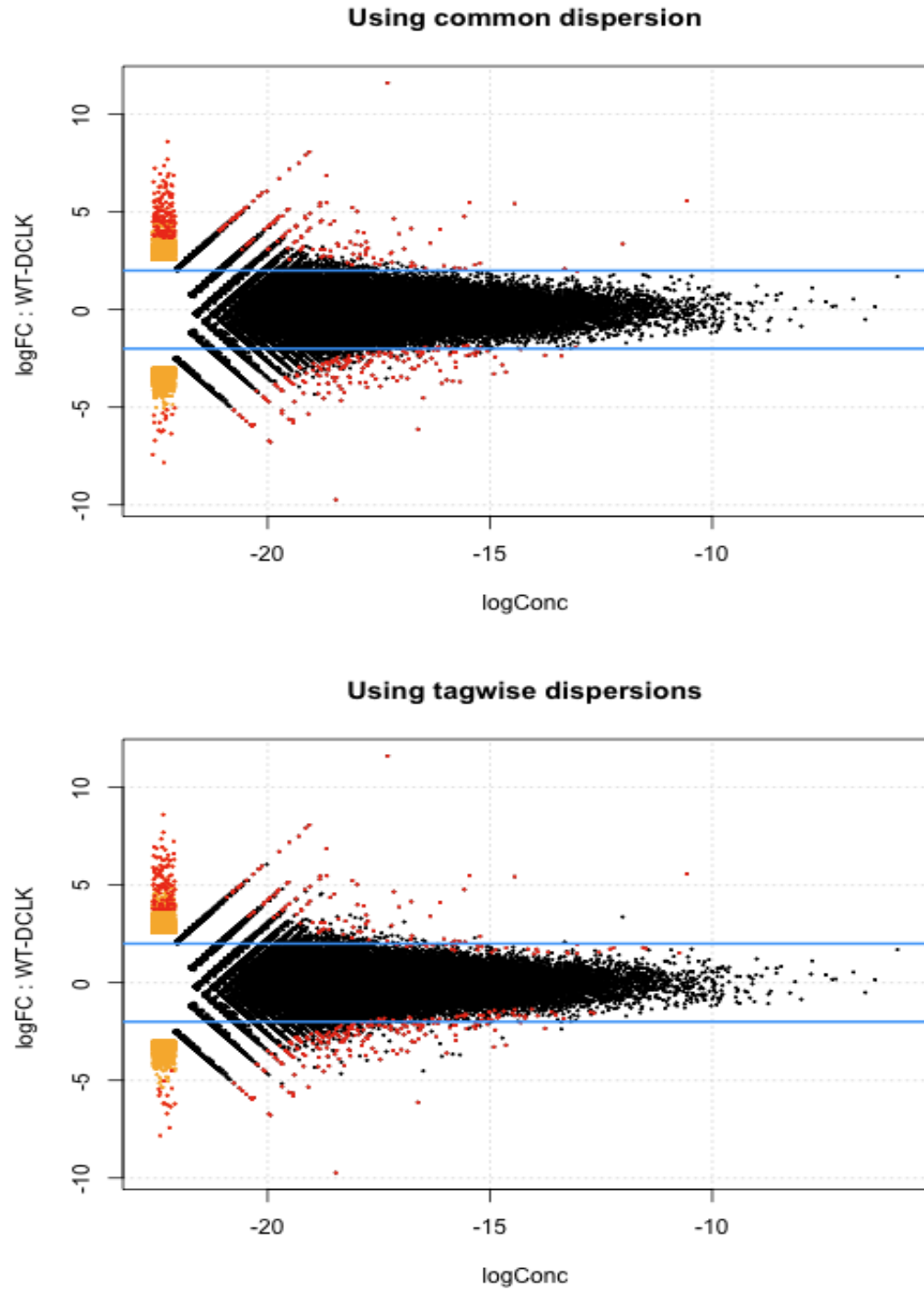


Figure 4: Plots of the log-fold change against the log-concentration for each tag, using the common dispersion (upper), and tagwise dispersions (lower). Tags with positive fold-change here are up-regulated in wild-type compared with transgenic mice. The 500 most differentially expressed tags according to each method are highlighted in red on both plots.

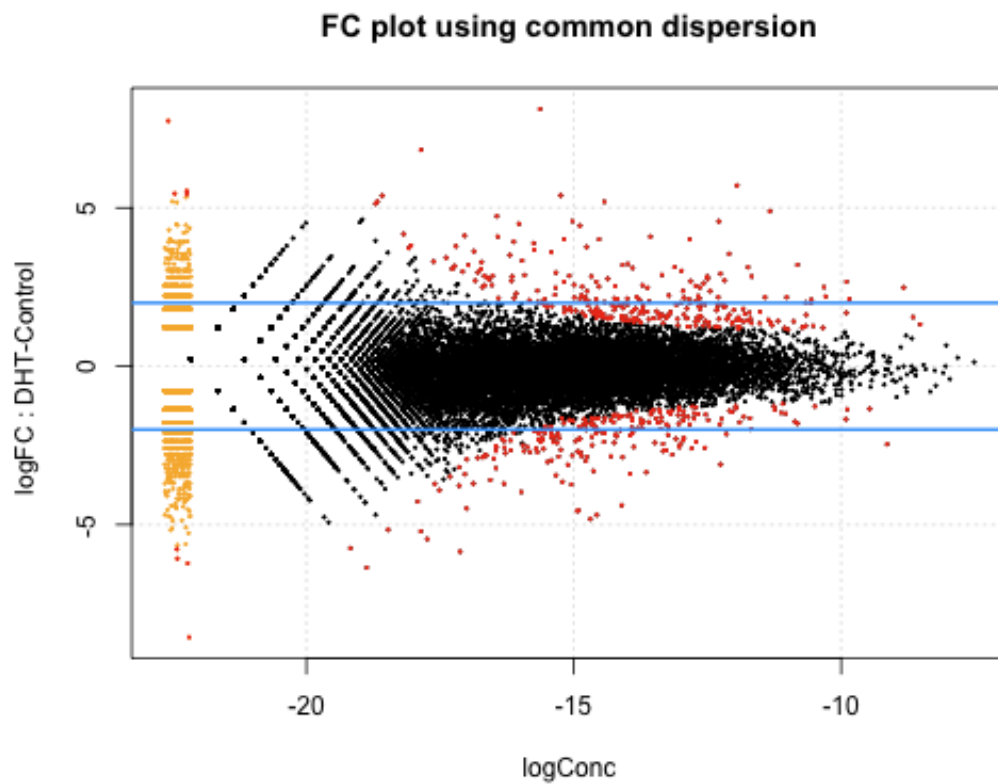


Figure 5: Plot of the log-fold change against the log-concentration for each tag. The 500 most differentially expressed tags as identified by `edgeR` using the common dispersion are outlined in red.



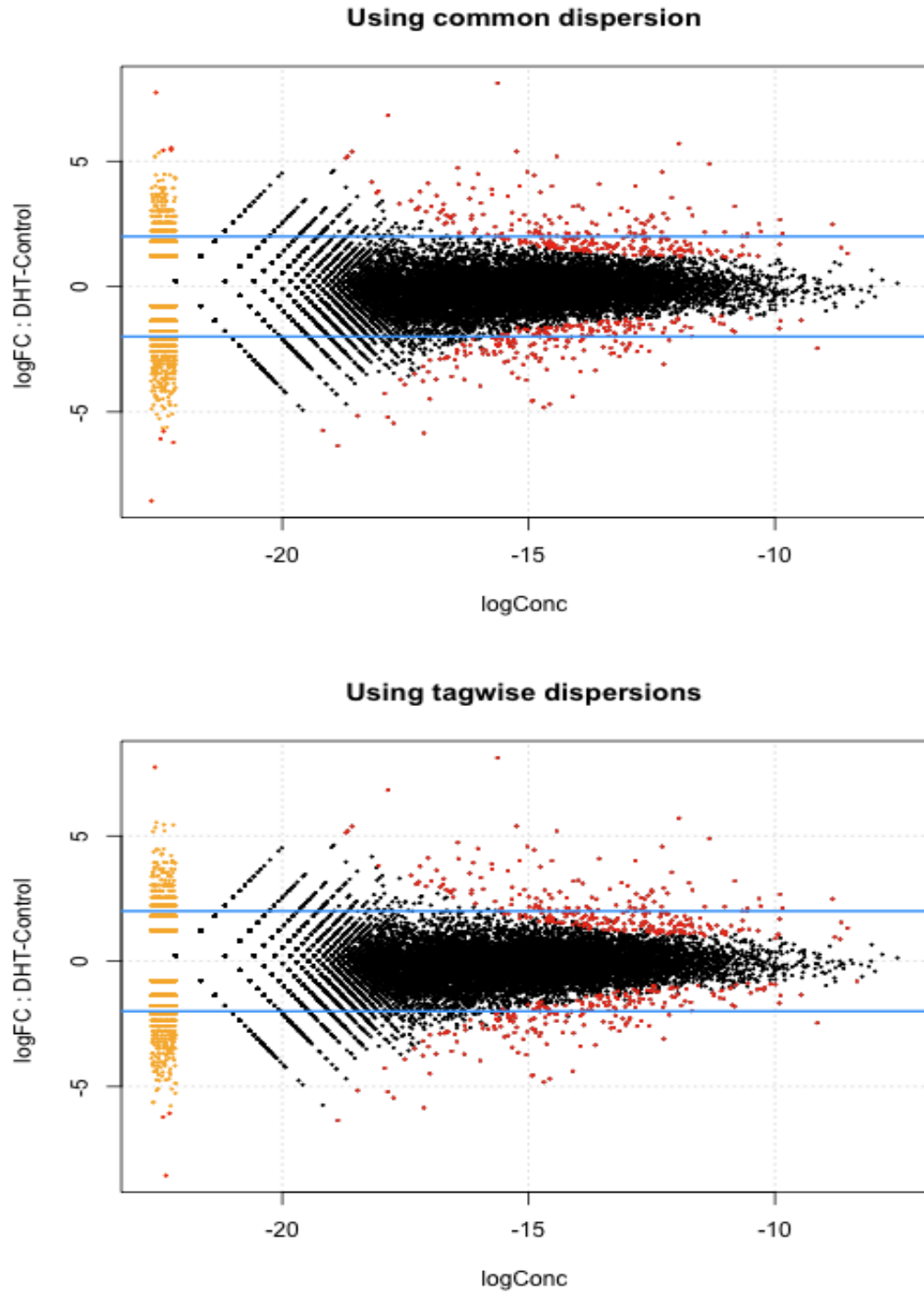


Figure 6: Plots of the log-fold change against the log-concentration for each tag, using the common dispersion (top), and tagwise dispersions (bottom). Tags with positive fold-change here are up-regulated in DHT-treated cells compared with control cells. The 500 most differentially expressed tags according to each method are highlighted in red on both plots.